



Separator Ion Optics School

NSCL, Michigan State University

Series of Four Lectures plus COSY Tutorials
September 10-14, 2018

Georg P. Berg
University of Notre Dame
JINA Center for the Evolution of the Elements

The Lecture Series

An Introduction to Ion-Optics

1st Lecture: 9/10/18: Formalism and ion-optical elements

2nd Lecture: 9/12/18: Ion-optical systems and spectrometers

3rd Lecture: 9/12/18: Recoil separators for nuclear astrophysics, St. GEORGE

4rd Lecture: 9/13/18: The recoil separator SECAR for FRIB

Tutorials in the afternoon: 9/10/18 – 9/14/18: COSY Infinity

Review 2nd Lecture

Ion-optical systems, spectrometers

High resolution spectrometers

Full dispersion matching

Diagnostics and field measurements.

Observing faint radiation near the sun:

An analogy for observing nuclear particles close to the beam

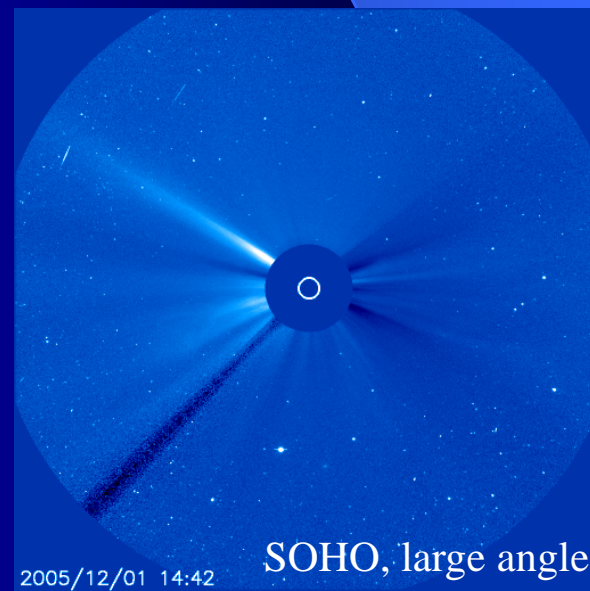
Solar Eclipse Coronagraph



Shadow of moon of Earth



Solar Eclipse 1999



2005/12/01 14:42

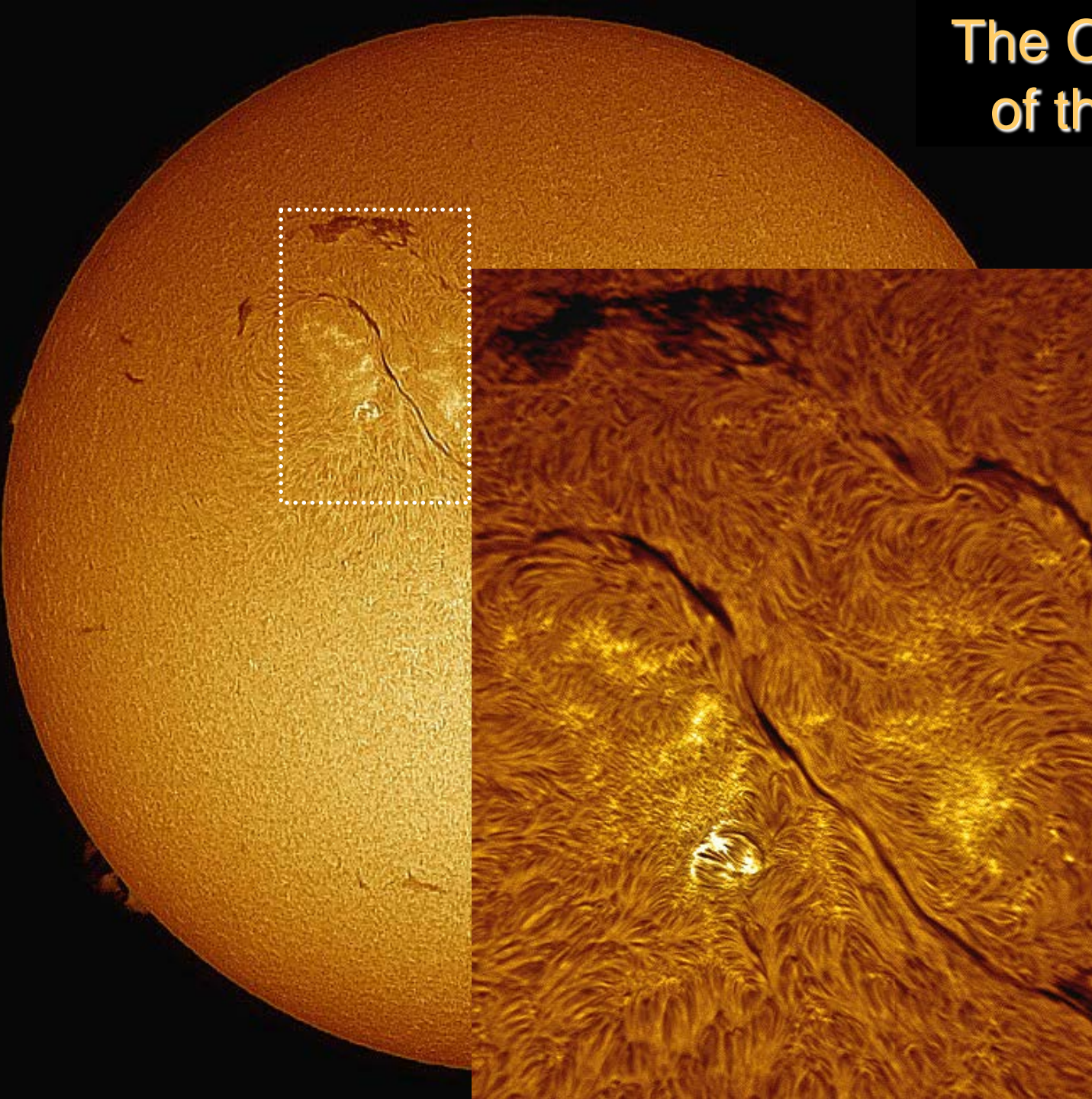
SOHO, large angle

The Chromosphere of the Sun in H α

H α line, $\lambda = 656.28\text{nm}$

$\Delta\lambda = 0.07\text{nm}$

Narrow Band Filter



Magnetic ($B\rho$) Separation of Beam & Reaction Products in Spectrometer Experiments near 0°

K600, Grand Raiden Spectrometers:

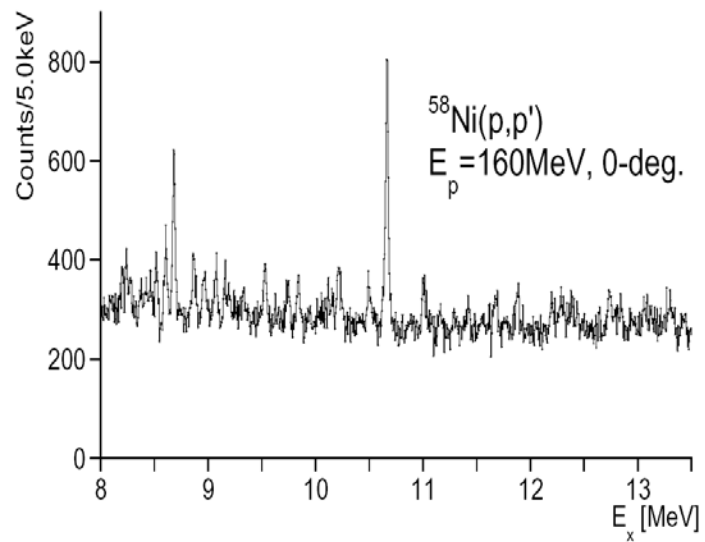
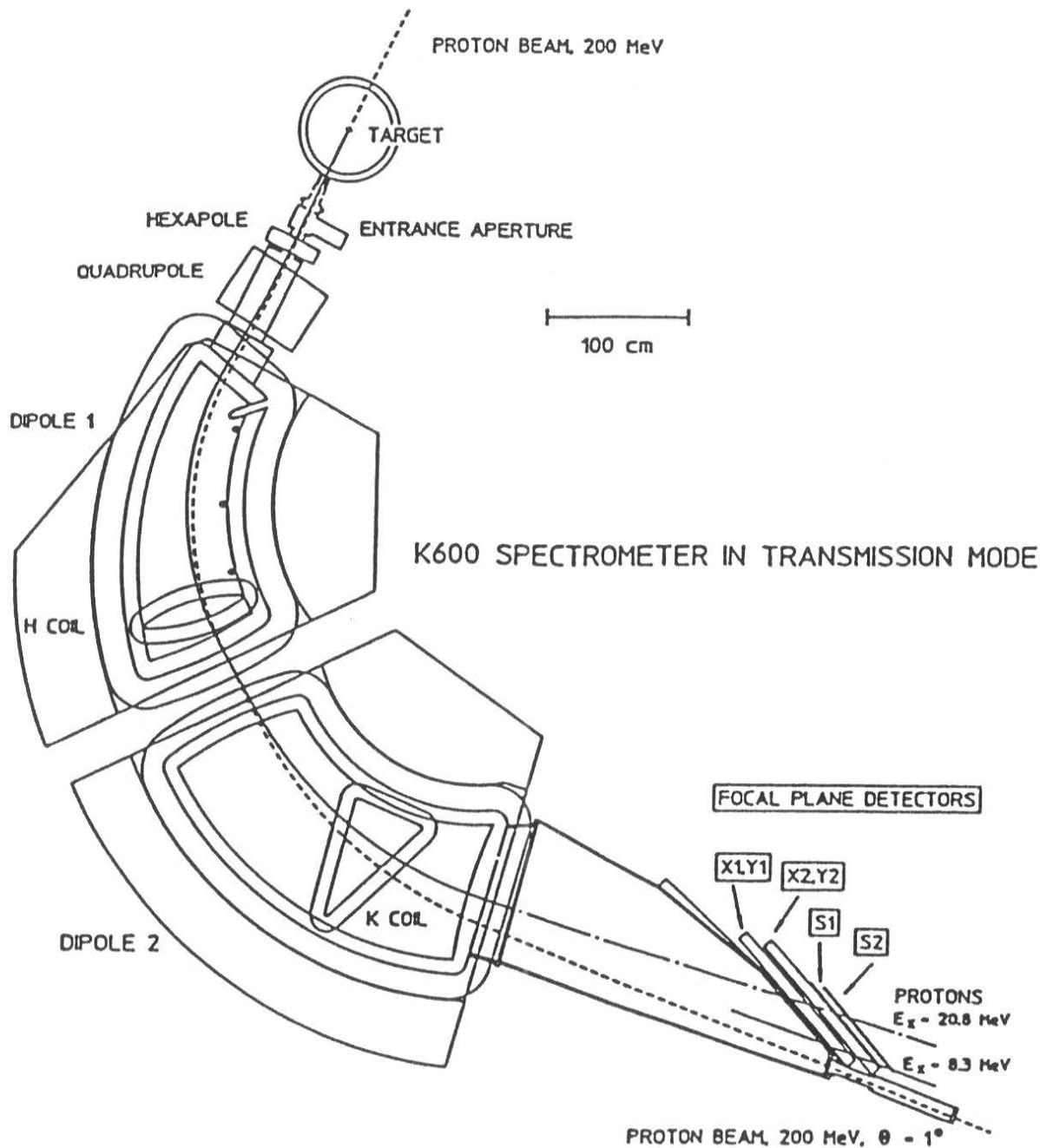
$({}^3\text{He}, t)$, (p, t) , (α, α') , (p, p') , $(\alpha, {}^8\text{He})$

Special Faraday cups to stop beam
inside spectrometer or near focal plane

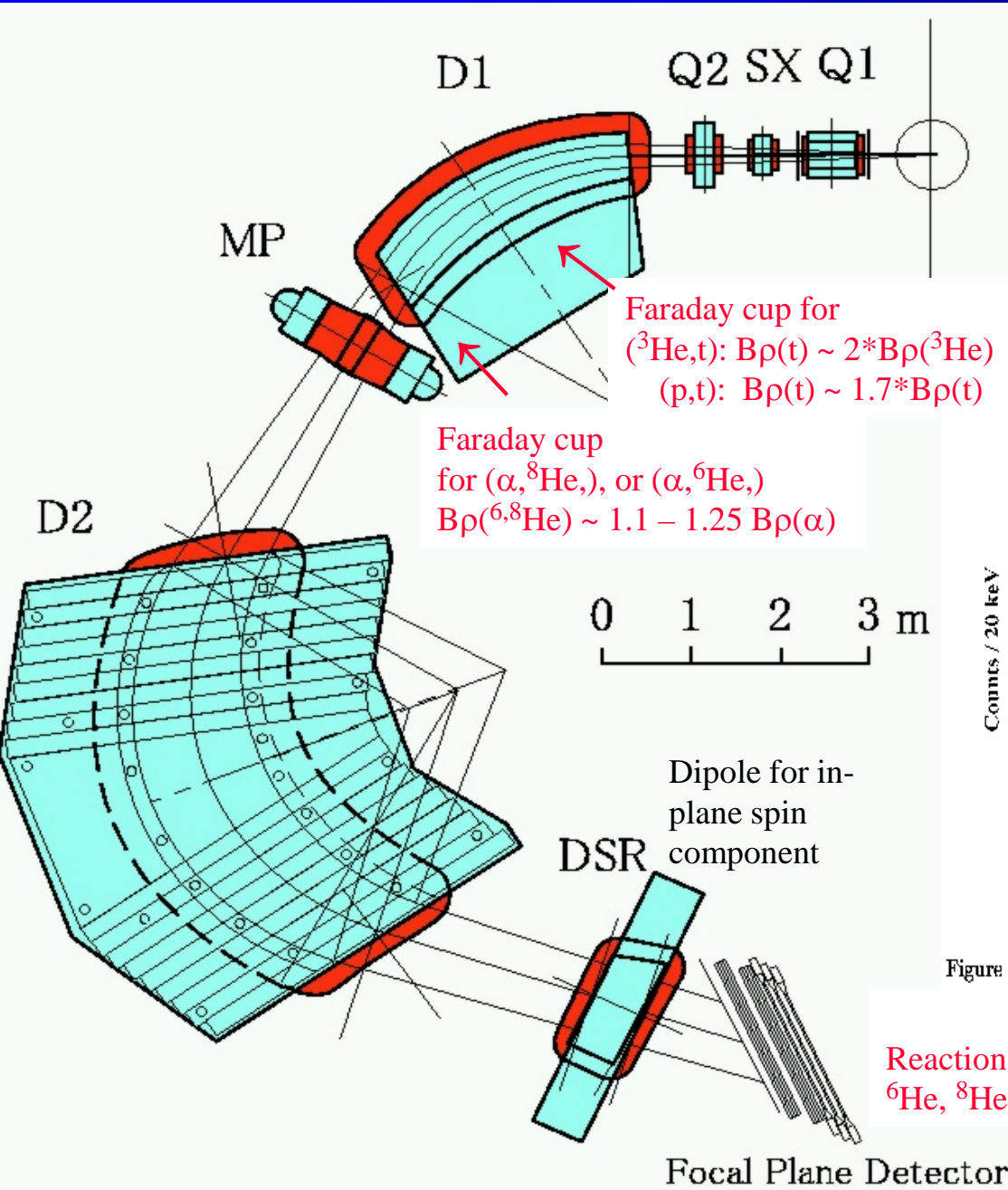
K600 Spectrometer (IUCF)

The K600 is shown in
 0° Transmission mode
for inelastic scattering
at 0°

High Dispersion Plane
 $B(D1) > B(D2)$



Grand Raiden High Resolution Spectrometer



Grand Raiden is shown in 0° Transmission mode for reactions at 0°

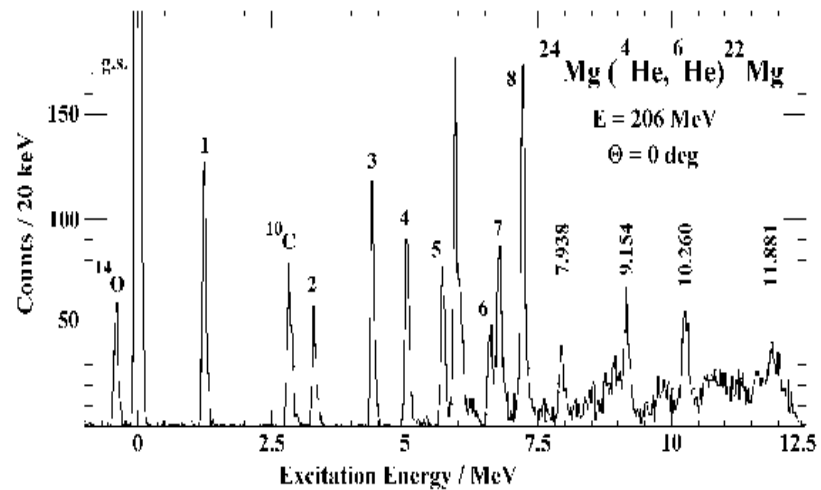
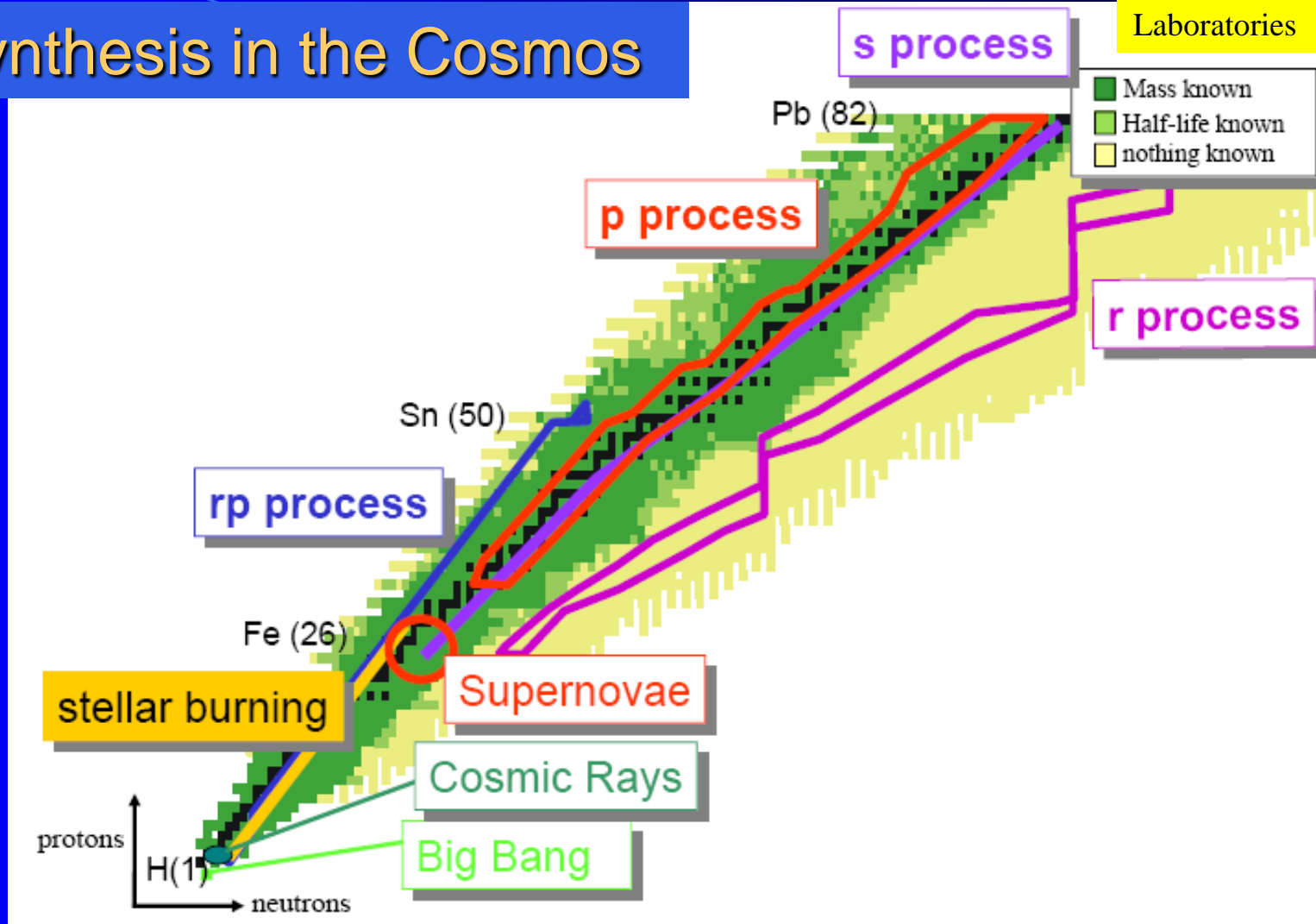


Figure 1. Measured ^{22}Mg spectrum with angle cut $0 - 1.5^\circ$ and a resolution of 75 keV.

Reaction Products
 $^6\text{He}, ^8\text{He}, t$

Nucleosynthesis in the Cosmos



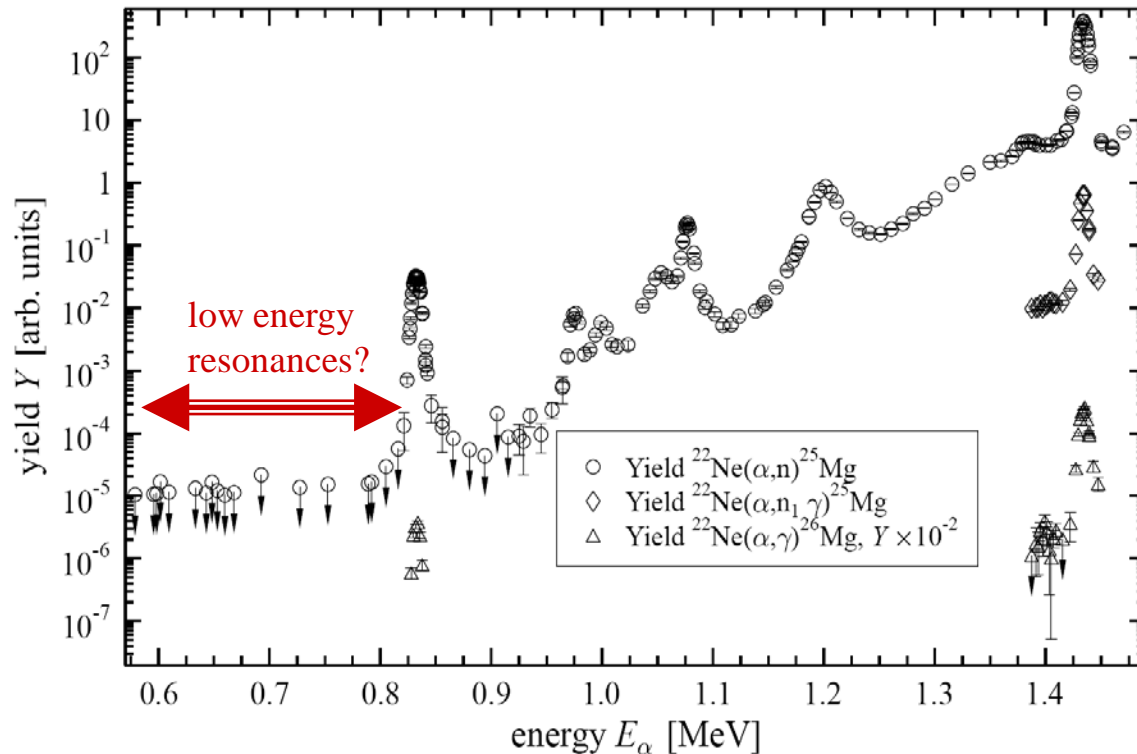
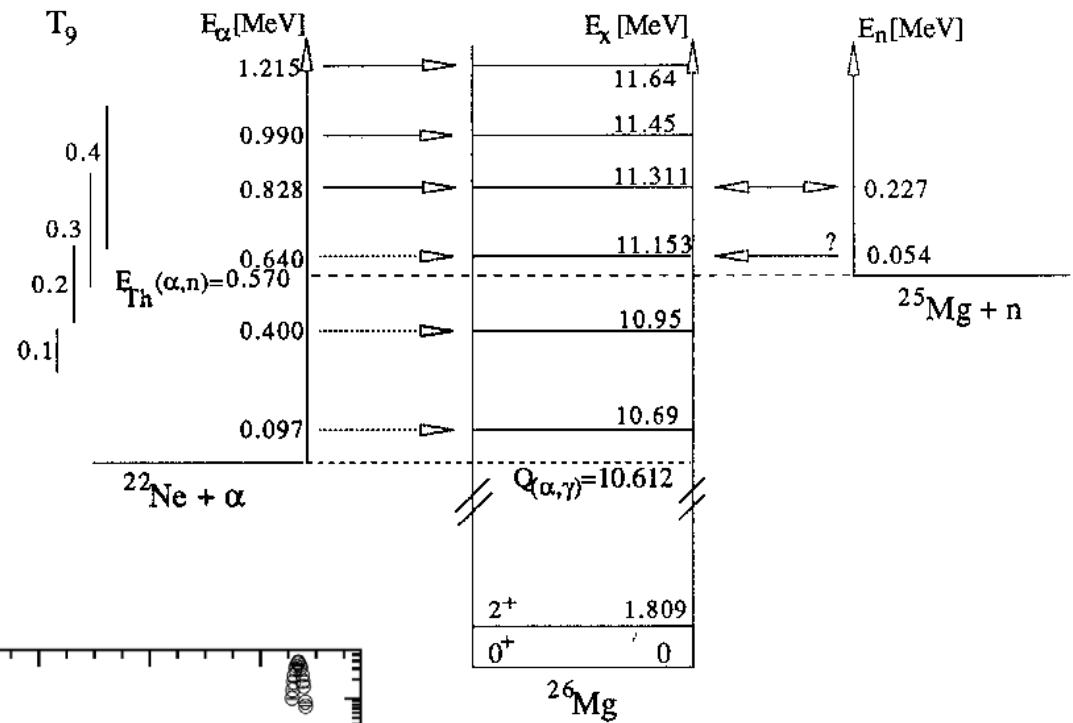
Many different reactions are involved in the nuclei synthesis

With recoil separators, we study the important (p,γ) and (α,γ) radiative capture reactions that take place e.g. in the rp process.

Example: $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$, $^{22}\text{Ne}(\alpha, \gamma)^{26}\text{Mg}$

The potential existence of low energy resonances causes considerable uncertainty in reaction rate

Stable Beams: St. GEORGE
RI Beams: SECAR



Low energy resonances

Cannot be measured due to low cross sections that do not rise above background from:

- 1) Cosmic rays
- 2) Surrounding radio-active materials
- 3) Beam-related background

Solutions:

- 1) Go underground (Salt mine!)
- 2) Inverse kinematics (recoil separator)

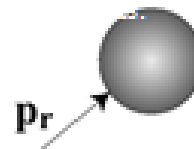
Rigidity and Acceptance Parameters Determined by Reaction Kinematics and Target Effects

Radiative capture (p,γ) , (α,γ) in inverse kinematics

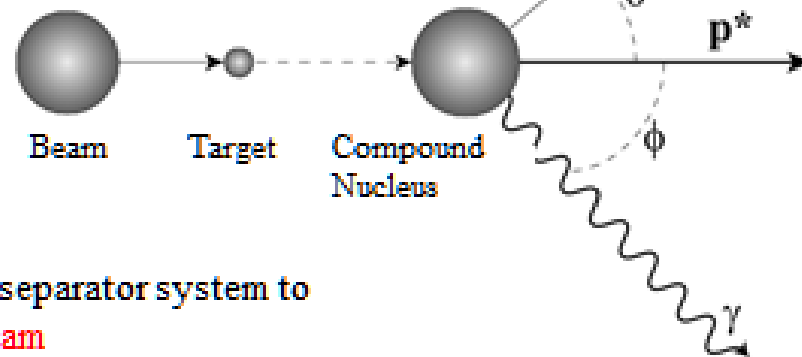
Kinematics of productions

Recoil maximum aperture:

$$\theta_{\max} = \arctan\left(\frac{p_\gamma}{p^*}\right) = \arctan\left(\frac{E_\gamma/c}{\sqrt{2m_s E_s}}\right)$$

$$p_r = p^* \pm p_\gamma$$


Most of the beam does not interact



Need a recoil separator system to

- Reject the beam
- Transport the recoils in a detector

Slide by Manoel Couder

Table 1

Design parameters of the St. George magnetic recoil separator.

Maximum rigidity $B\rho$	0.45 Tm
Minimum rigidity $B\rho$	0.1 Tm
Angle acceptance, vert., horiz	± 40 mrad
Energy acceptance	± 7.5 %
Mass separation $m/\Delta m$	≈ 100
Bending radius	75 cm



Beam and recoils have same momenta, need E field for separation.

Table 2

Sample of reactions of astrophysical interest

		Inverse (α, γ) reaction								
Beam	Recoil	Beam E_{lab} MeV	E_{cm} MeV	Recoil E_{lab} MeV	Recoil Q[9]	Recoil Abund. %	Half Angle mrad	E Range \pm %	Mom. p MeV/c	$B\rho$ T/m
^{16}O	^{20}Ne	5.80	1.16	4.640	5	42	14.2	2.8	415.7	0.277
		12.5	2.50	10.02	6	40	11.8	2.4	610.9	0.340
^{18}O	^{22}Ne	1.94	0.35	1.591	3	38	39.2	7.8	177.1	0.284
		3.30	0.60	2.700	4	42	30.9	6.2	332.6	0.277
^{34}S	^{38}Ar	10.0	1.05	8.950	8	32	10.4	2.1	795.7	0.332
		38.0	4.00	34.00	12	32	7.20	1.4	1551	0.431
^{36}Ar	^{40}Ca	12.5	1.25	11.25	9	31	9.10	1.8	915.3	0.339
		40.0	4.00	36.00	13	30	6.70	1.3	1638	0.420

St. George

Reactions and Design Parameters

Achromatic magnet separator

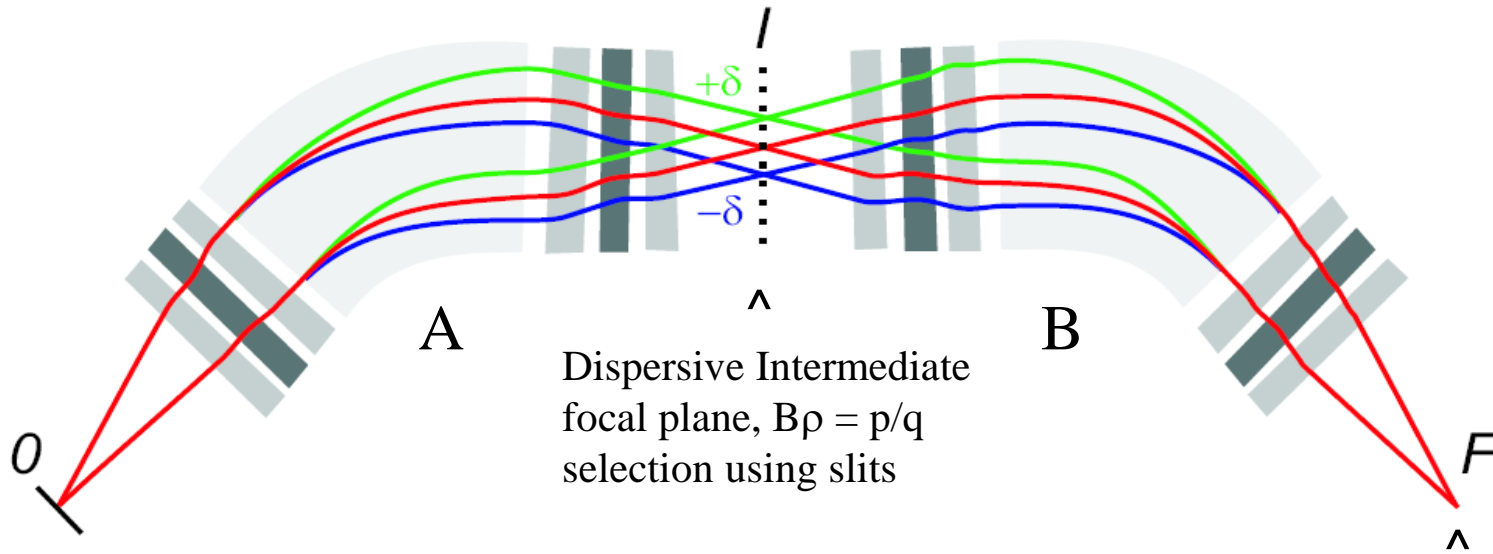


Figure from Experimental Techniques at NSCL, MSU, Th. Baumann, 8/2/2002

Achromatic Final focal plane, small beam spot e.g. for detector system

Assume foci at I & F, i.e. $A_{12} = B_{12} = 0$.
Derive the first order achromatic condition of the system $0 \rightarrow F$ and compare with the dispersion matching condition.

First order
TRANSPORT
Matrix $R_{\mu\nu}$

$$\begin{array}{c}
 \begin{array}{l}
 \text{Magnification } M_x \\
 \downarrow \\
 \begin{bmatrix} x(t) \\ \theta(t) \\ y(t) \\ \varphi(t) \\ l(t) \\ \delta(t) \end{bmatrix} \\
 \downarrow \\
 \vec{x}_2
 \end{array}
 =
 \begin{array}{c}
 \begin{array}{l}
 \text{Focusing fct} \\
 \downarrow \\
 \begin{bmatrix} R_{11} & R_{12} & 0 & 0 & 0 \\ R_{21} & R_{22} & 0 & 0 & 0 \\ 0 & 0 & R_{33} & R_{34} & 0 \\ 0 & 0 & R_{43} & R_{44} & 0 \\ R_{51} & R_{52} & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \\
 \downarrow \\
 \text{TRANSPORT-R-Matrix}
 \end{array}
 \cdot
 \begin{array}{c}
 \begin{array}{l}
 \text{Lateral Dispersion} \\
 \downarrow \\
 \begin{bmatrix} R_{16} \\ R_{26} \\ 0 \\ 0 \\ R_{56} \\ 1 \end{bmatrix} \\
 \downarrow \\
 \vec{x}_1
 \end{array}
 \begin{array}{l}
 x_0 \\ \theta_0 \\ y_0 \\ \varphi_0 \\ l_0 \\ \delta_0
 \end{array}
 \end{array}
 \end{array}
 \quad (2)
 \end{array}$$

Angular Disp

Solution of Exercise

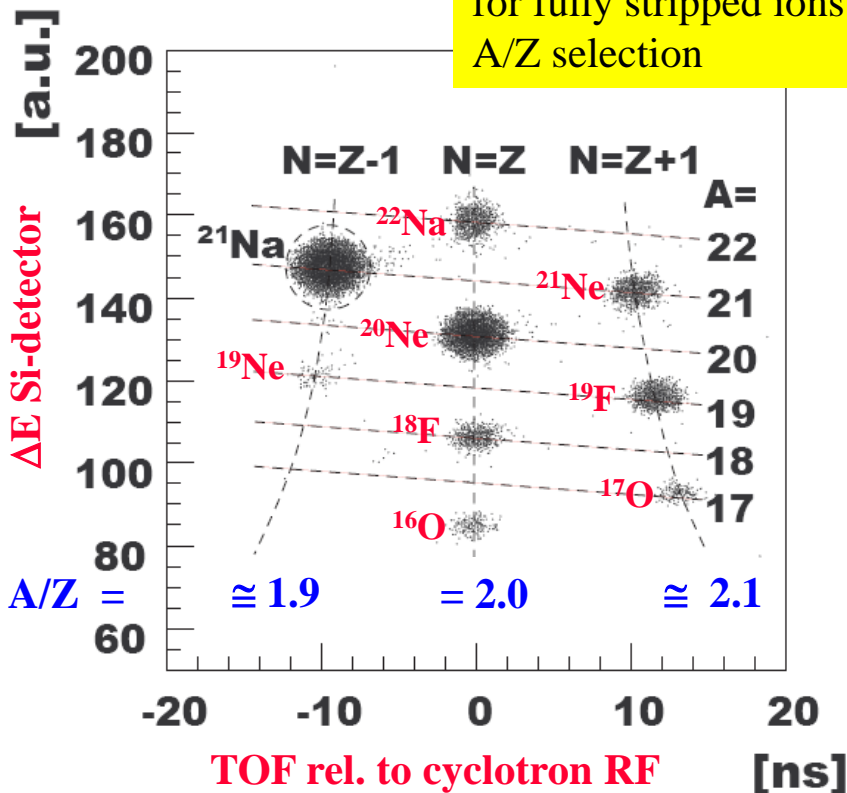
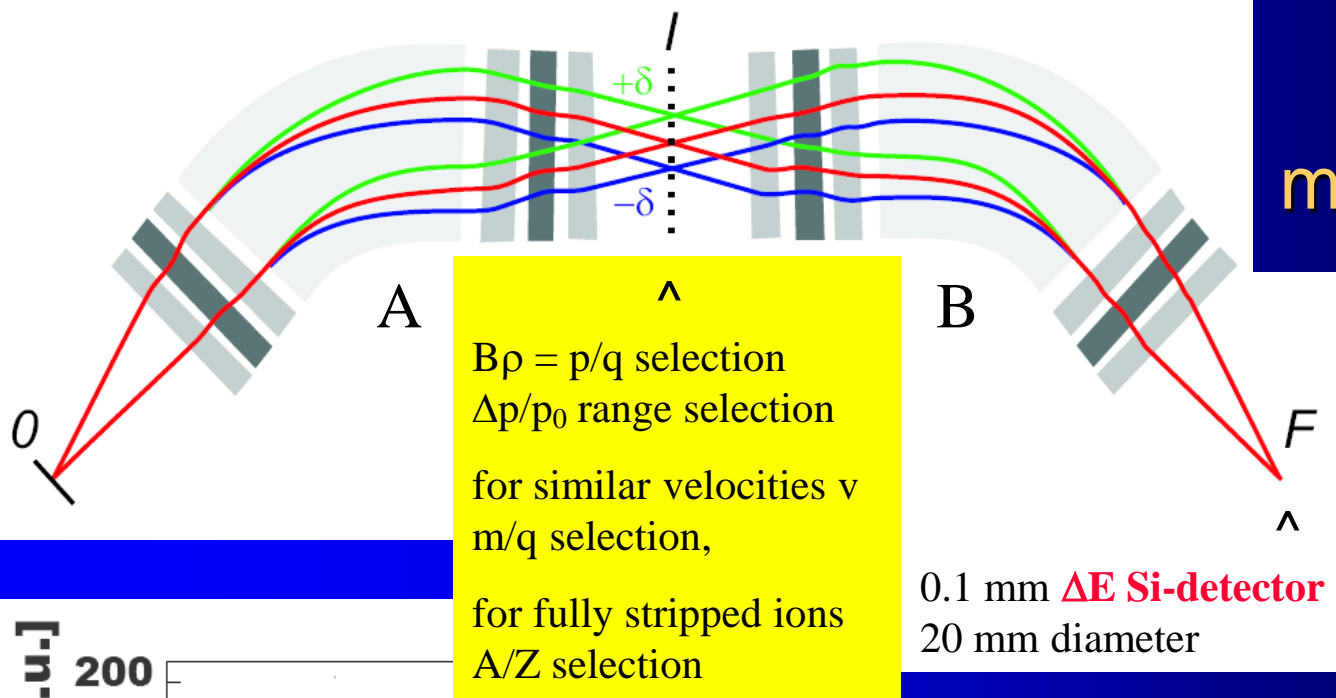
$$\begin{aligned}
 x_I &= A_{11} x_0 + A_{12} \theta_0 + A_{16} \delta_0 & | A_{12} &= 0 \\
 &= A_{11} x_0 + A_{16} \delta_0 & (25)
 \end{aligned}$$

$$\begin{aligned}
 x_F &= B_{11} x_I + B_{12} \theta_I + B_{16} \delta_0 & | B_{12} &= 0 \\
 &= B_{11} x_I + B_{16} \delta_0 & | \text{ substitute } x_I \text{ using } (25) \\
 &= B_{11} (A_{11} x_0 + A_{16} \delta_0) + B_{16} \delta_0 \\
 &= B_{11} A_{11} x_0 + (B_{11} A_{16} + B_{16}) \delta_0
 \end{aligned}$$

Condition for achromaticity: $A_{16} = -B_{16} / B_{11}$

Note: This is the Dispersion Matching condition for $C = T = 1$

Achromatic magnet separator



Example: Production of ²¹Na via H(²¹Ne,n)²¹Na with ²¹Ne⁷⁺ beam at 43MeV/nucleon using the TRIμP Separator, KVI Groningen
 Ions after target fully stripped e.g. ²¹Ne¹⁰⁺ !

²¹Ne beam with ≈ 10¹⁰ ions/s with Bρ(²¹Ne)/ Bρ(²¹Na) ≈ 1.09 is all but eliminated by a slit (SH2) in front of plane I

Note:
 Ions with A/Z ~ 2 are not separated !

Achromatic magnet separator with Wedge

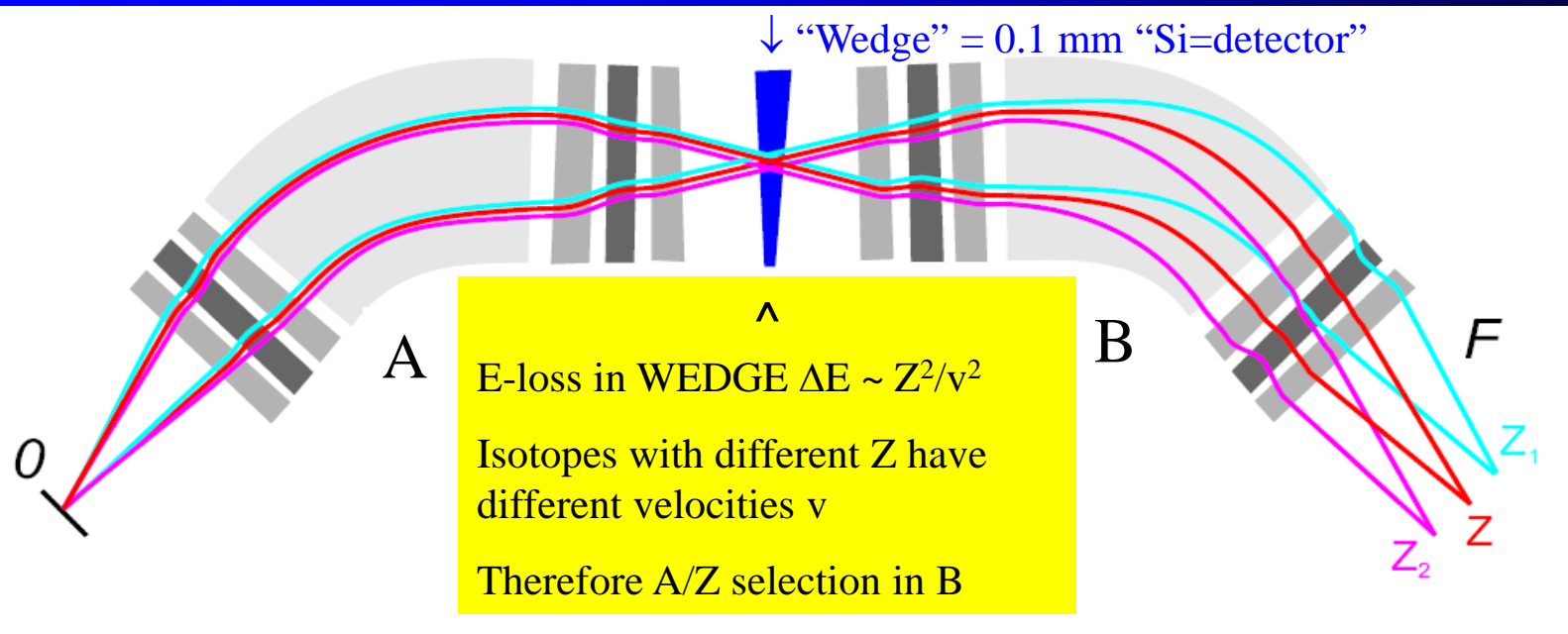
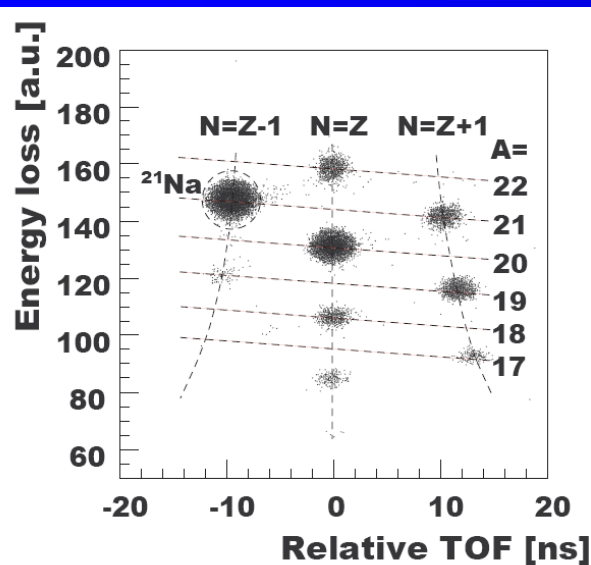


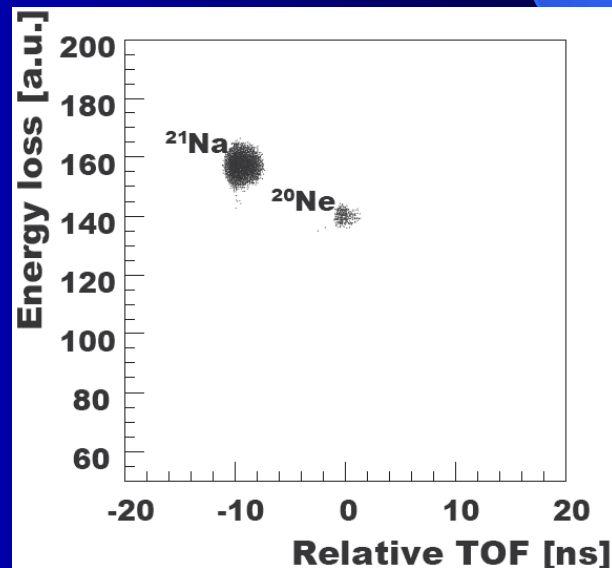
Figure from Experimental Techniques at NSCL, MSU, Th. Baumann, 8/2/2002



Effect of “Wedge” \Rightarrow

Note:

For large dp/p) the degrader should be Wedge-shaped to restore achromaticity effected by degrader with constant thickness

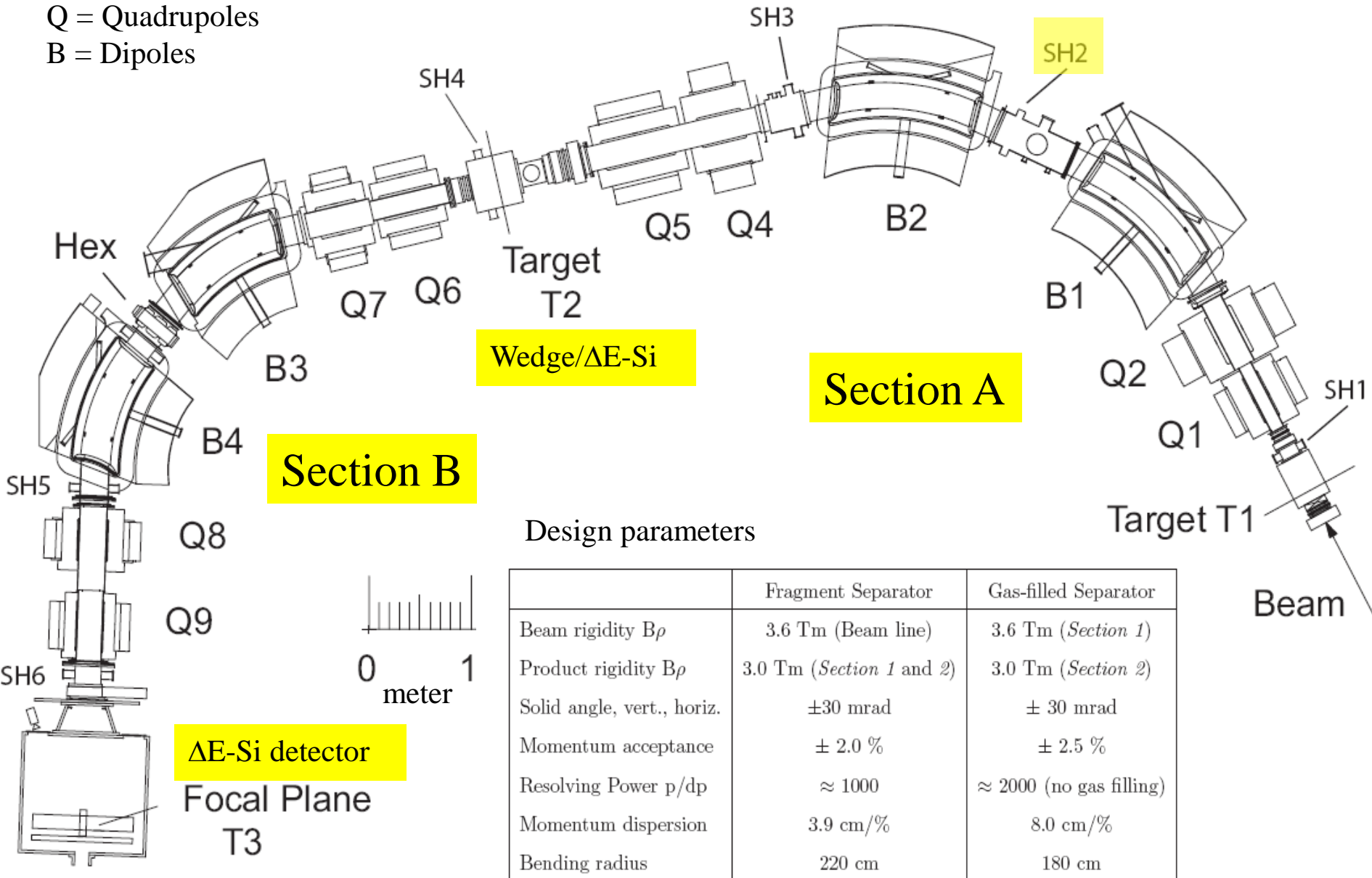


TRI μ P an achromatic secondary beam separator

SH = Slits

Q = Quadrupoles

B = Dipoles



Wedge/ ΔE -Si

Section A

Section B

Design parameters

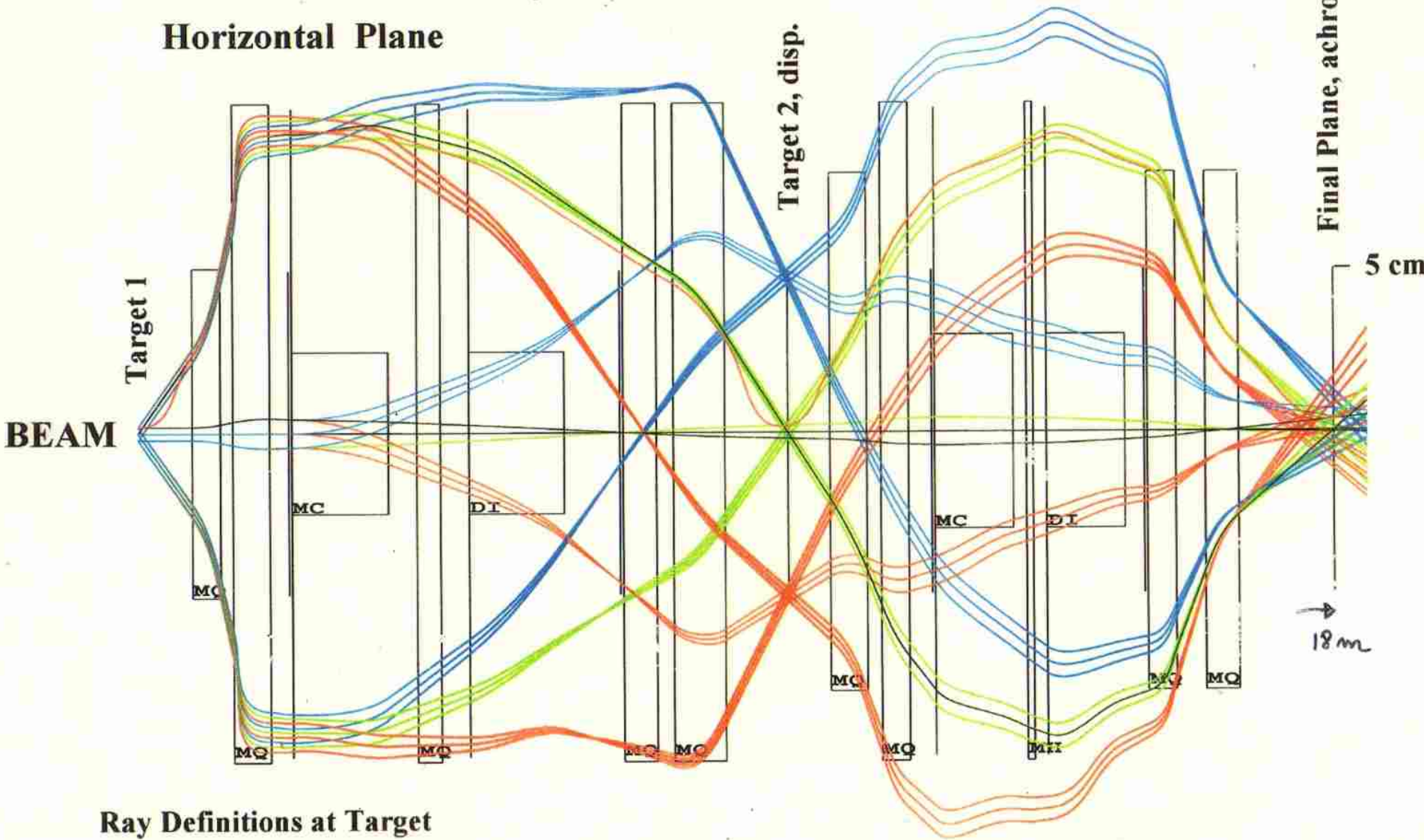
	Fragment Separator	Gas-filled Separator
Beam rigidity $B\rho$	3.6 Tm (Beam line)	3.6 Tm (<i>Section 1</i>)
Product rigidity $B\rho$	3.0 Tm (<i>Section 1 and 2</i>)	3.0 Tm (<i>Section 2</i>)
Solid angle, vert., horiz.	± 30 mrad	± 30 mrad
Momentum acceptance	± 2.0 %	± 2.5 %
Resolving Power p/dp	≈ 1000	≈ 2000 (no gas filling)
Momentum dispersion	3.9 cm/%	8.0 cm/%
Bending radius	220 cm	180 cm

TRIμP Fragment Separator

3rd order COSY Infinity Calculation

Horizontal Plane

TRIμP ion-optics



Ray Definitions at Target

- $x \cong \pm 2 \text{ mm}$
- $\theta = \pm 30 \text{ mrad}$
- $dp = \pm 2.5 \%$

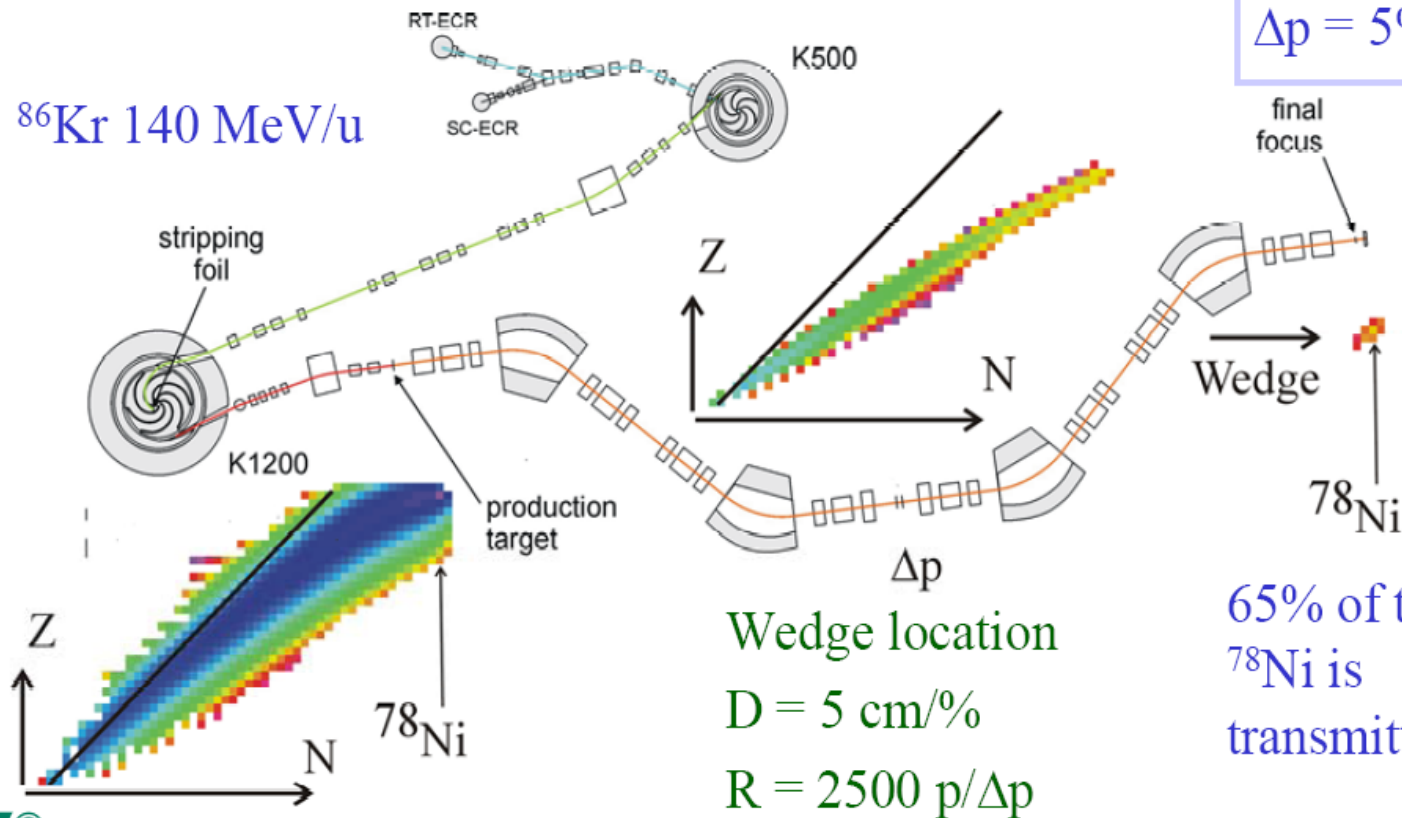
A1900 MSU/NSCL Fragment Separator

Overview of the Fragment Separation Technique

The NSCL Coupled Cyclotron Facility – A1900 Separator

8 msr
 $\Delta p = 5\%$

^{86}Kr 140 MeV/u

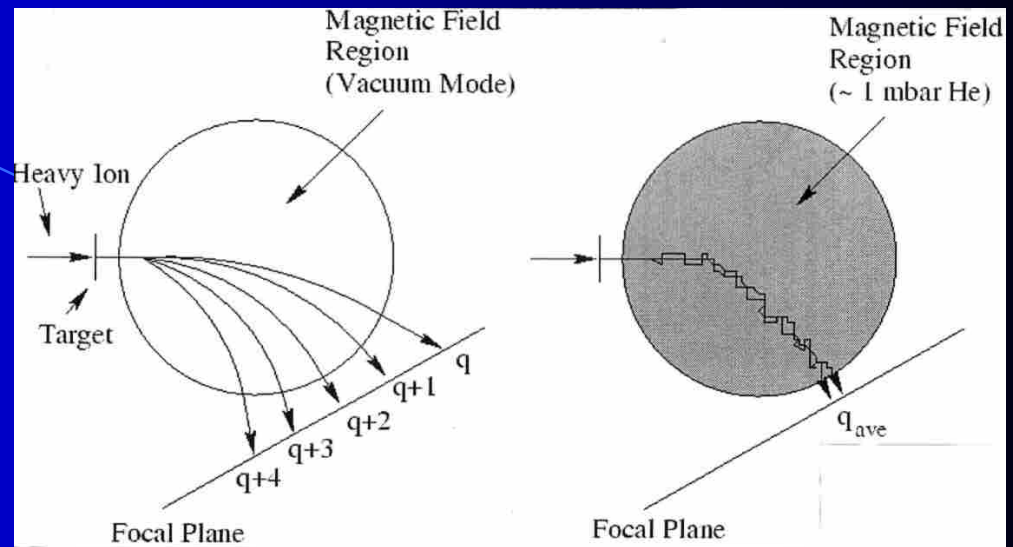


Another example are the BigRIPS Fragment Separator at RIKEN in Japan And the Super-FRS at GSI.

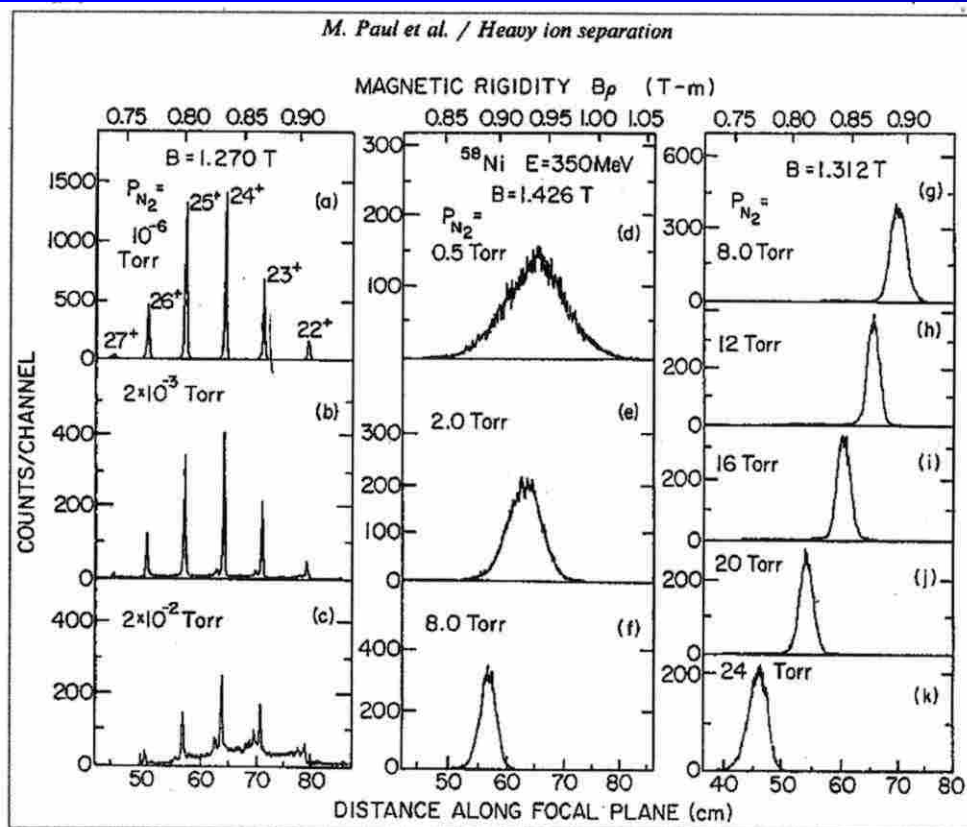
Gas-filled separators Concept

PROBLEM: After target, a distribution of several charge states q exists for low E or large Z , with $B\rho$ range typically larger than acceptance causing transmission losses.

REMEDY: gas-filled separator



M. Paul et al. / Heavy ion separation

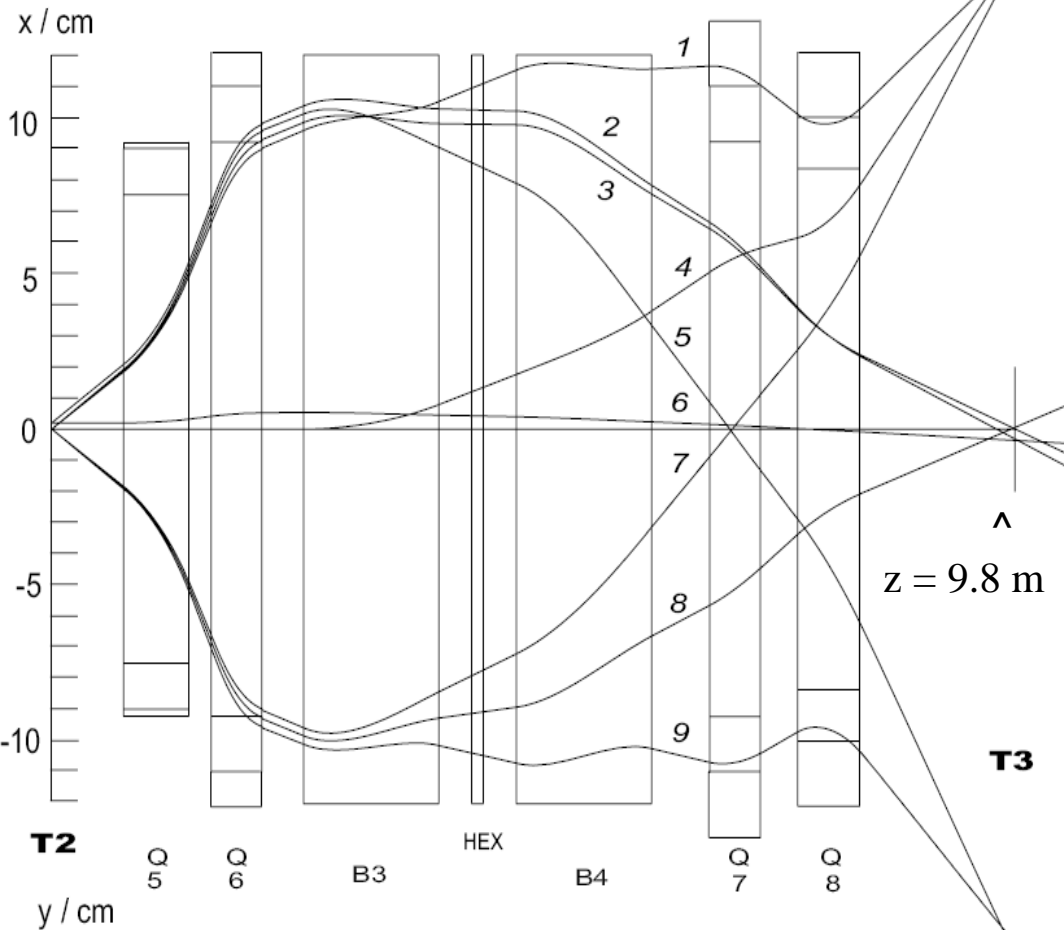


Rays in a magn. dipole field
without and with gas-filling

Measured spectra as function of
gas pressure (e.g. He, Ar)

TRIμP ion-optics Section B

A “long” achromatic separator system is not suitable for a gas-filled separator that should be “short” to reduce statistical E spread and have “large dispersion”

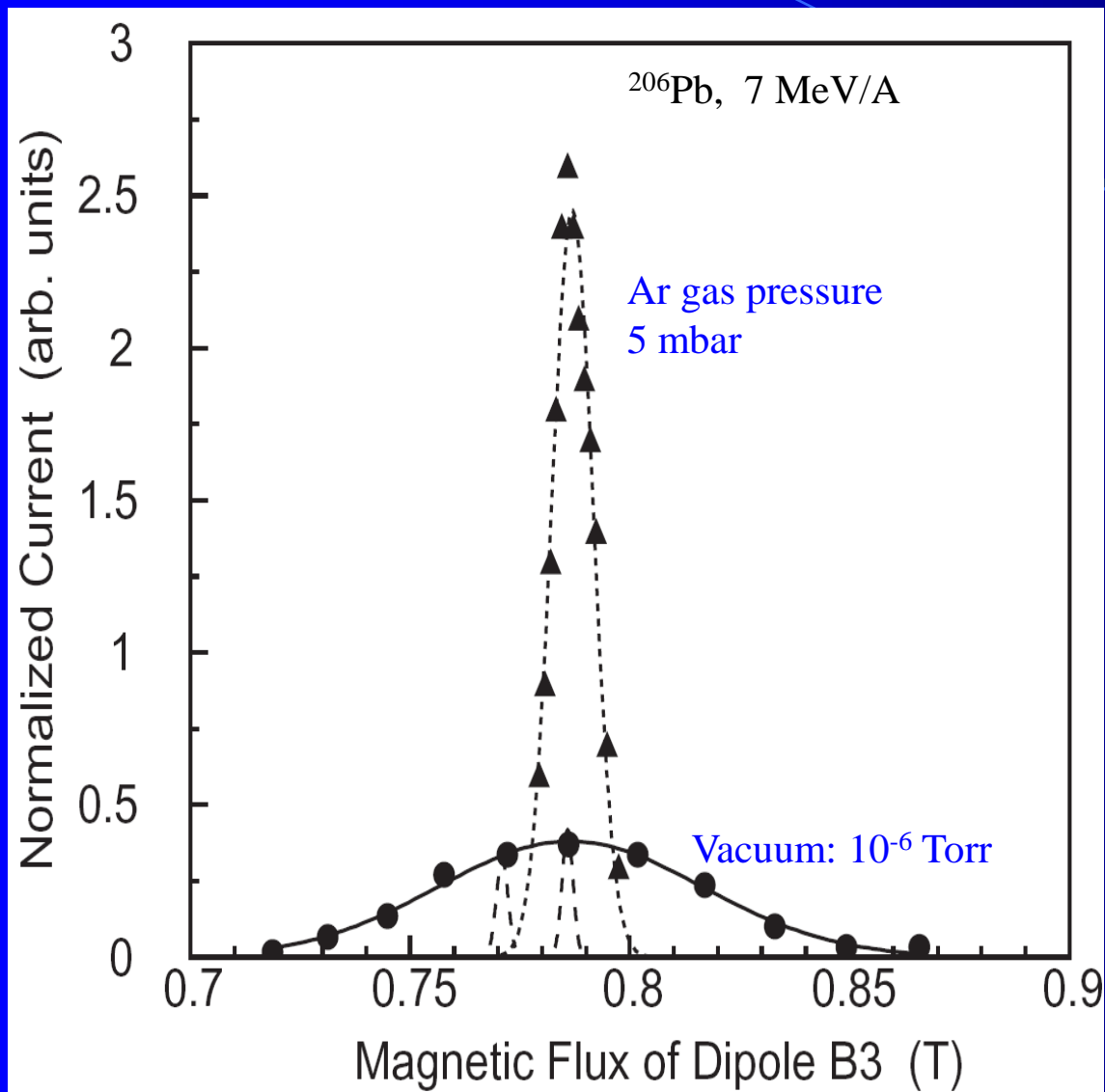


ray	x [mm]	Θ [mrad]	$\Delta E/E$ [%]	y [mm]	Φ [mrad]
1	0	30	4.0	-1.5	30
2	2	30	0	0	30
3	0	30	0	1.5	0
4	0	0	4.0	0	-30
5	0	30	-4.0	1.5	-30
6	2	0	0		
7	0	-30	4.0		
8	0	-30	0		
9	0	-30	-4.0		

Therefore:

The TRIμP separator was
Designed to be able operate
with Section A as beam line
& Section B as short gas-filled
separator with large dispersion

Charge state distribution in TRI μ P separator with gas-filling



Difference between Fragment and Recoil Separators

- ❖ Fragment separators use high energy beams to produce efficiently rare isotopes (RI).
- ❖ Recoil separators work at low energy to study astrophysical reactions.

CONSEQUENCES:

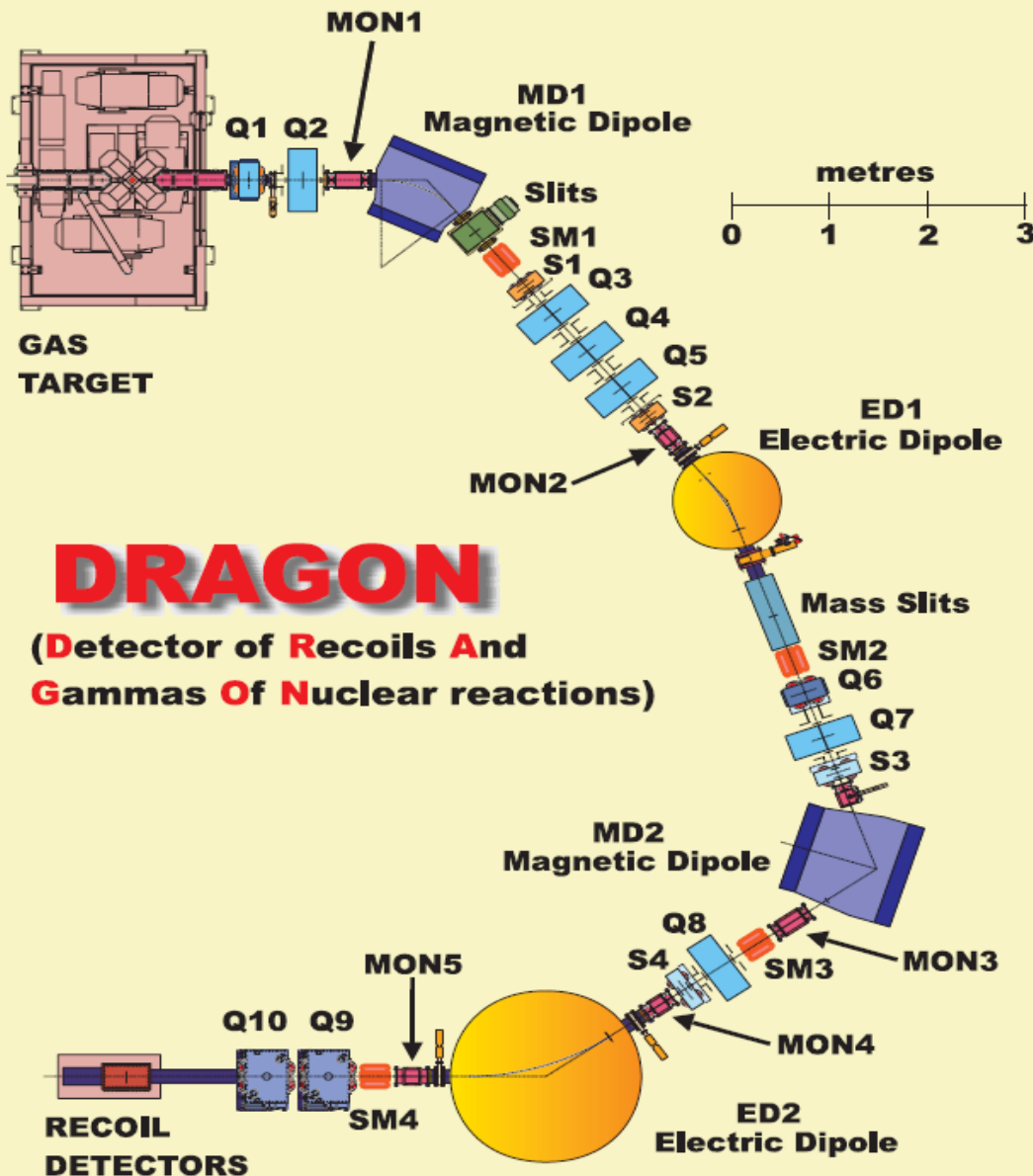
- ❑ Fragment separators use the ΔE loss in Wedges to separate RIs.
- ❑ Recoil separators use Electric fields to separate beam and recoils due to their mass differences. Either electric dipoles or Wien filters.

DRAGON

Recoil Separator with Electric Dipoles

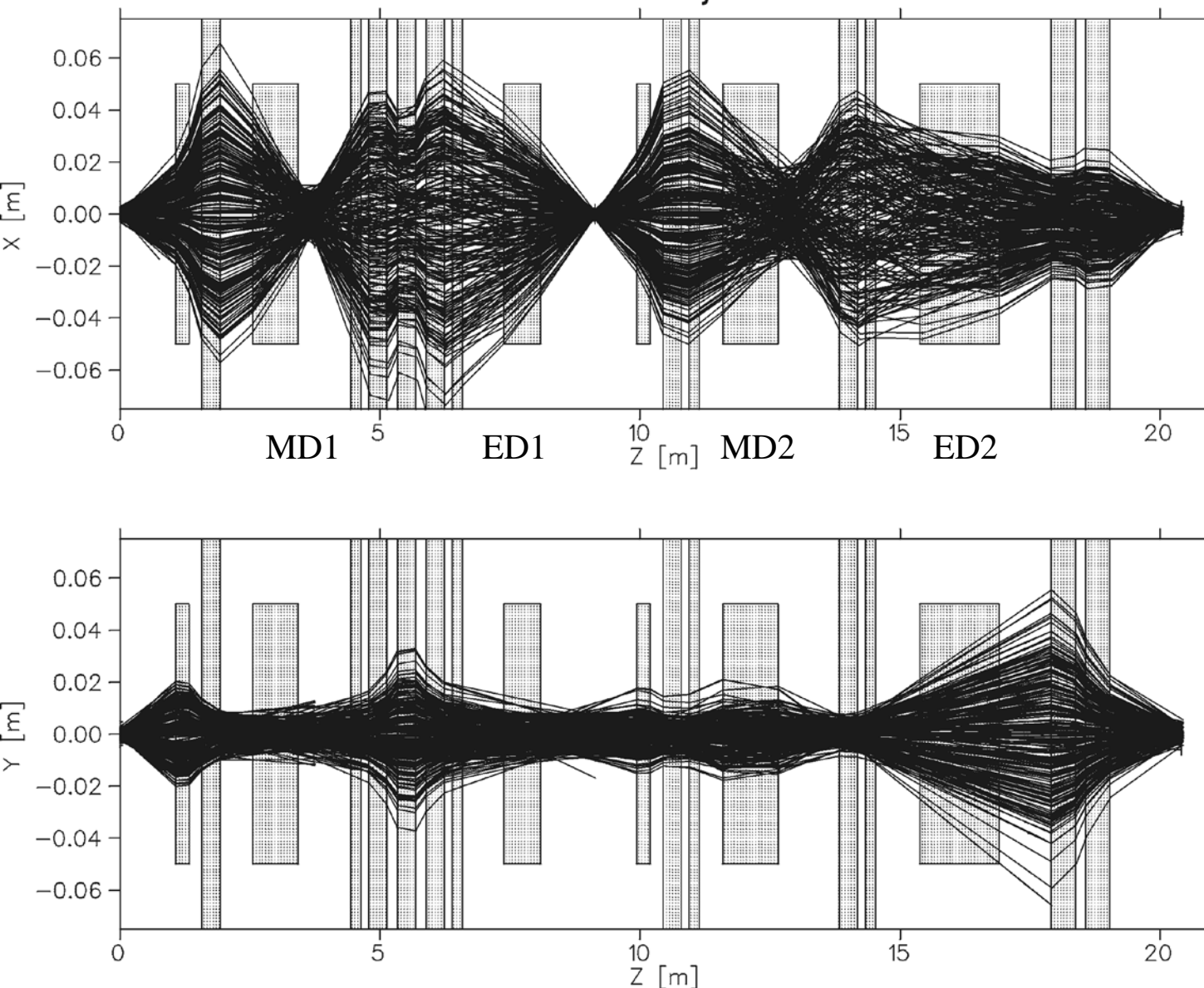
Study of astrophysics reactions using radioactive beams:

e.g. $^{21}\text{Na}(p,\gamma)^{22}\text{Mg}$ in inverse kinematics using a radioactive ^{21}Na beam of 4.62 MeV to study NeNa cycle



Ref. Dragon Recoil Separator Optics, The Recoil Group, 1/18/1999, TRIUMF

Horizontal and Vertical projections
of ^{19}Ne trajectories



EMMA

Recoil Separator for ISAC-II at TRIUMF

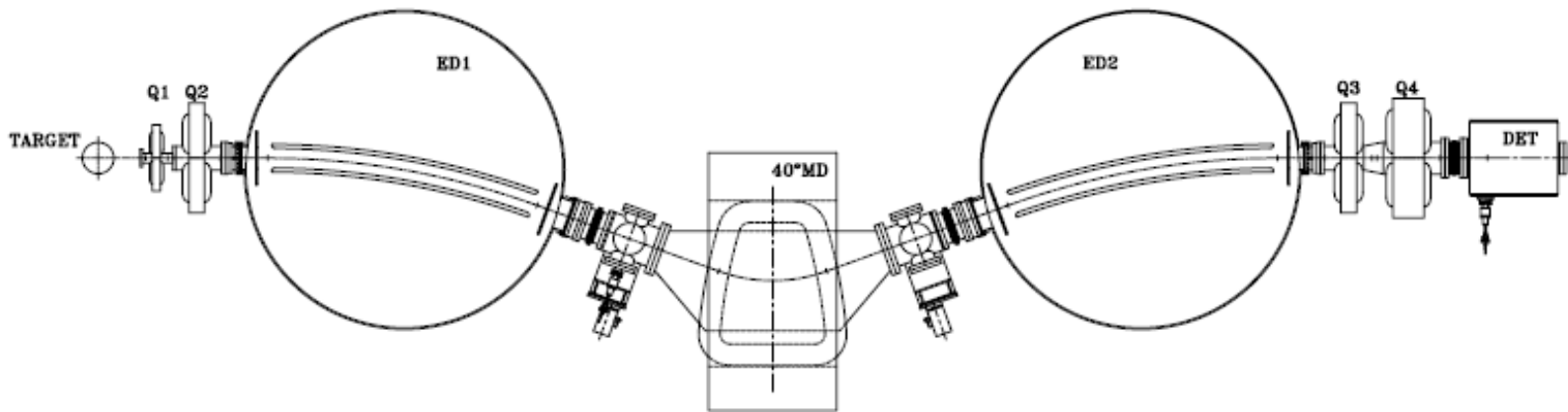
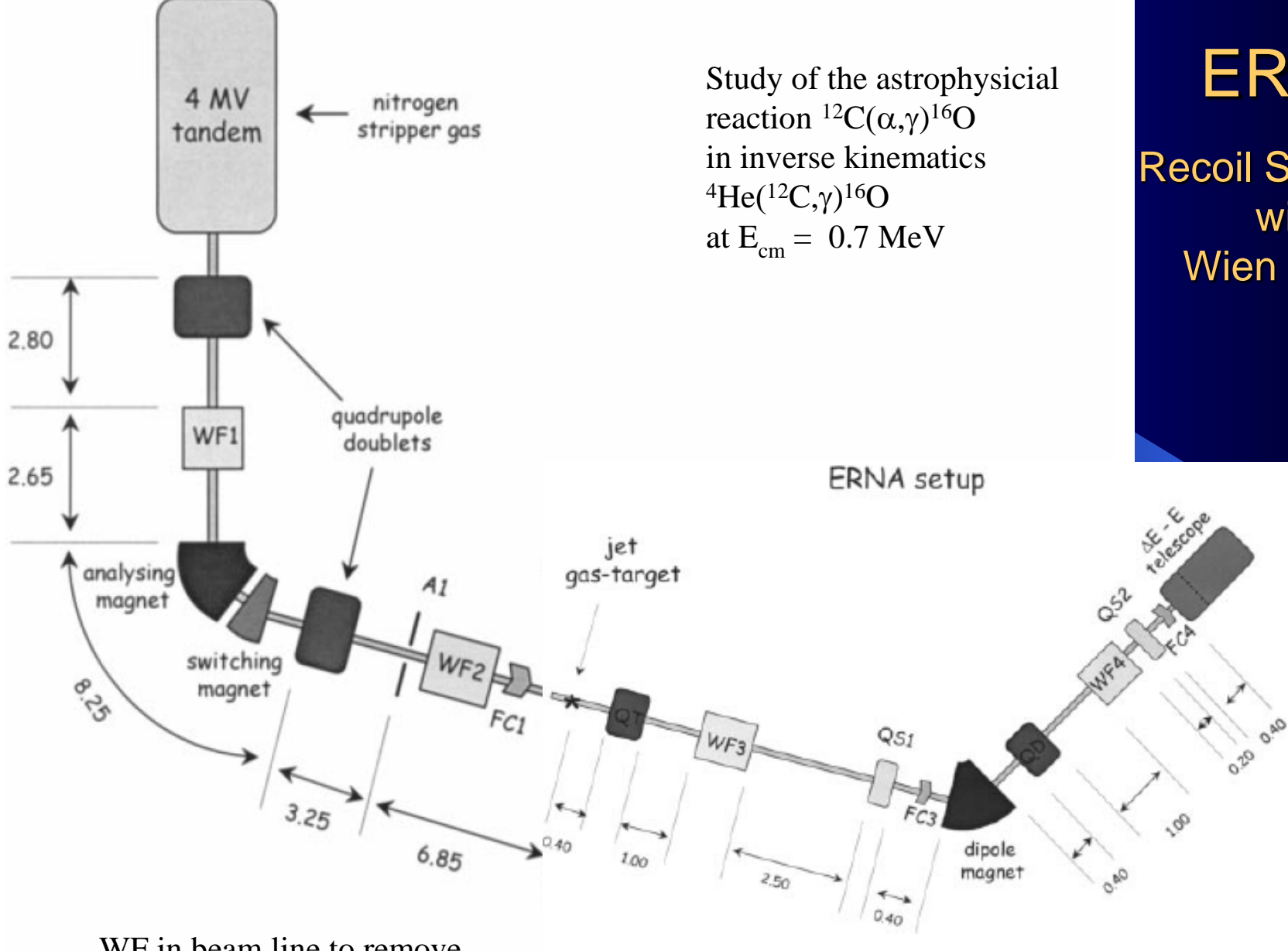


Fig. 1. Schematic view of EMMA, showing the target, quadrupole and dipole magnets, and electric dipoles. The detector box is also indicated.

ERNA

Recoil Separator with Wien Filters

Study of the astrophysical reaction $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ in inverse kinematics $^4\text{He}(^{12}\text{C},\gamma)^{16}\text{O}$ at $E_{\text{cm}} = 0.7 \text{ MeV}$



WF in beam line to remove ^{16}O contaminant in ^{12}C beam

beam purification

ERNA Recoil Separator with 2 Wien Filters WF3, WF4

ERNA

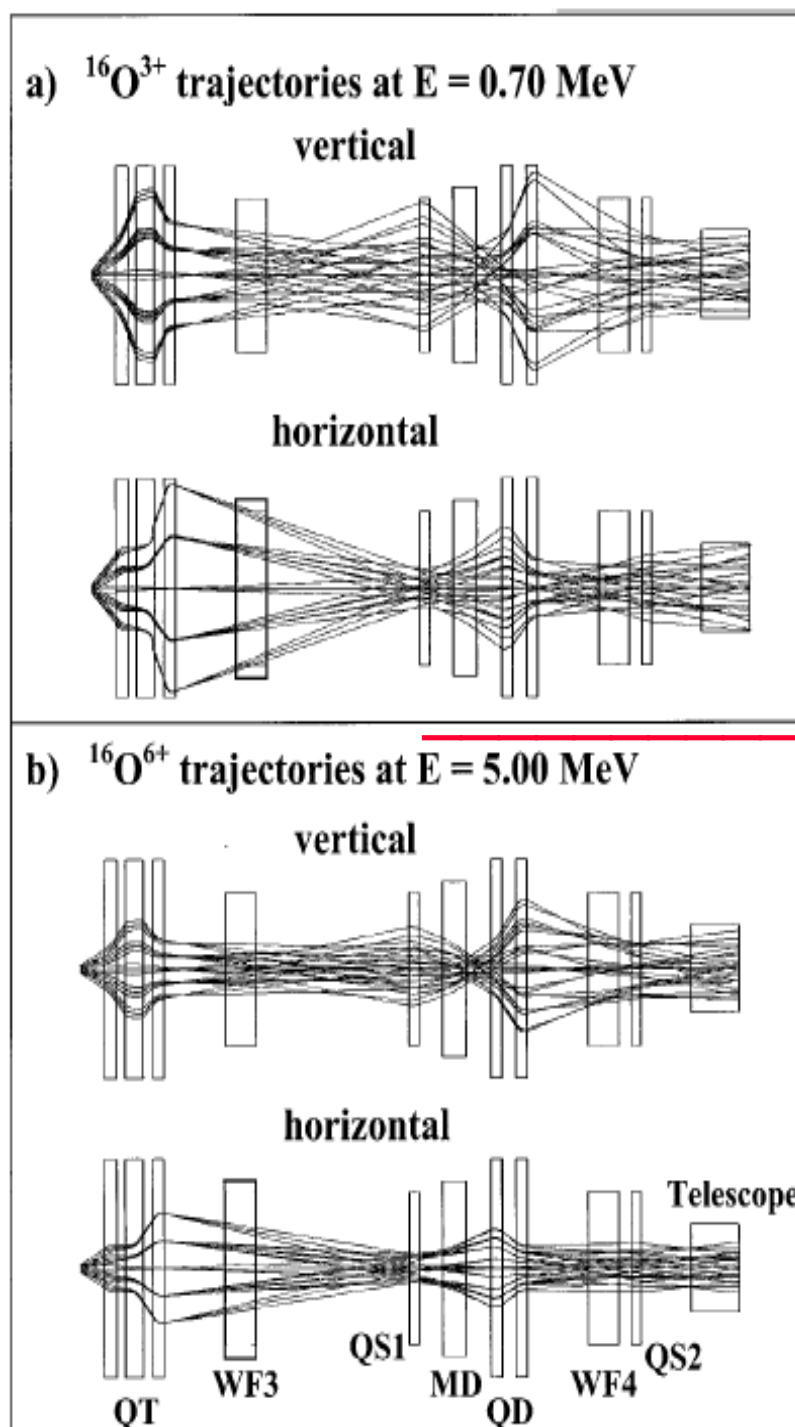
Recoil Separator
with
Wien Filters

Ion-optics of
 $^{16}\text{O}^{3+}$ and $^{16}\text{O}^{6+}$ ions

3rd order calculations using
COSY Infinity

^{12}C beam mainly stopped in
Faraday cup between QS1 and MD

Fig. 2. Samples of ^{16}O trajectories are shown for (a) $E = 0.70$ MeV ($q_0 = 3^+$, $\theta_{\text{max}} = 1.9^\circ$, $\Delta E = 0.13$ MeV) and (b) $E = 5.0$ MeV ($q_0 = 6^+$, $\theta_{\text{max}} = 1.0^\circ$, $\Delta E = 0.44$ MeV). The trajectories start at the jet gas-target (^4He target density = 1×10^{18} atoms/cm²) and are followed through the filtering and focusing elements of ERNA (indicated by square boxes) up to the telescope (WF = Wien filter, QS = quadrupole singlet, QD = quadrupole doublet, QT = quadrupole triplet, MD = magnetic dipole)



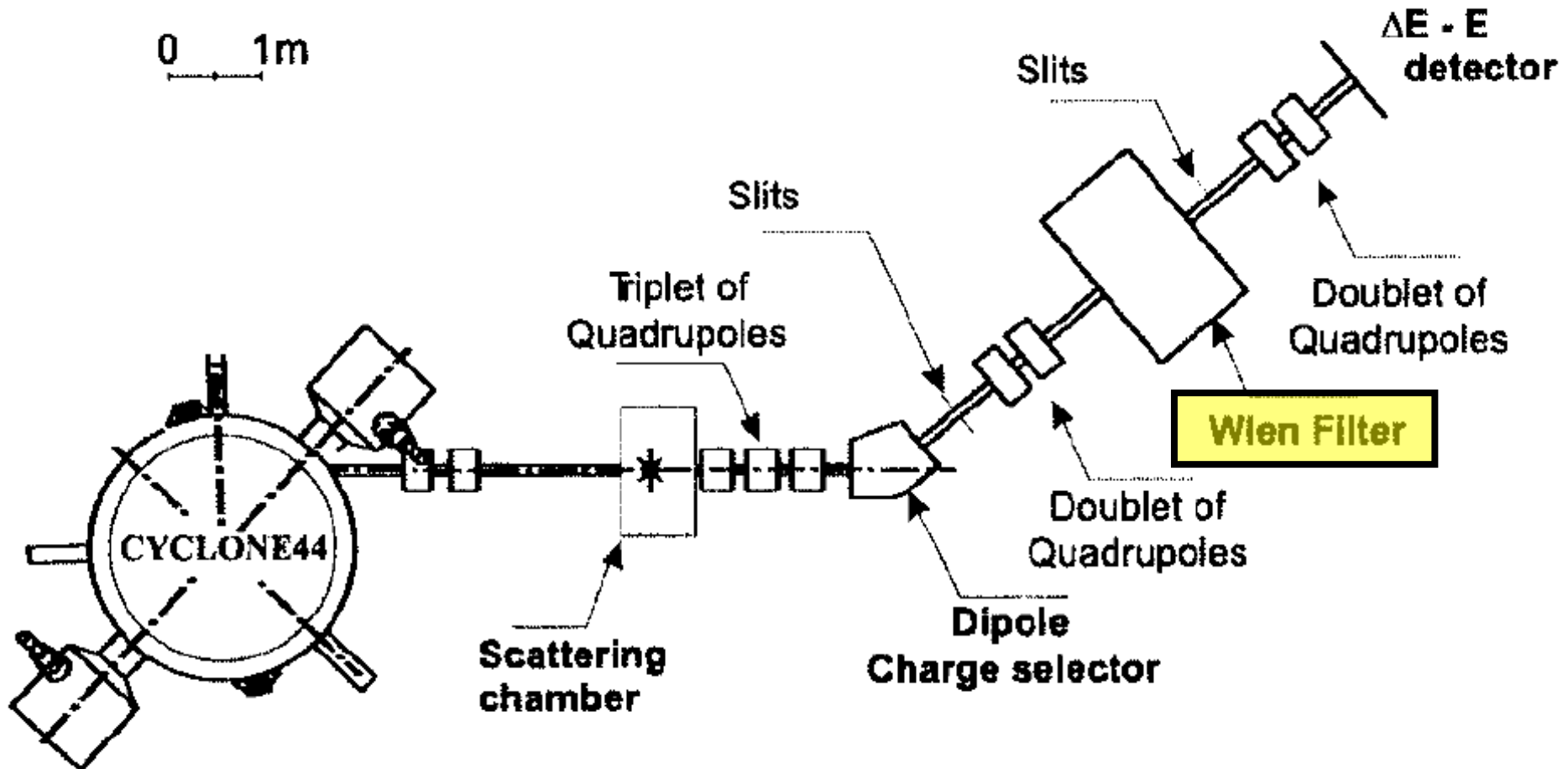
Study of astrophysics reactions using radioactive beams.

Example: Hot CNO breakout reaction $^{19}\text{Ne}(p,\gamma)^{20}\text{Na}$ in inverse kinematics using a radioactive ^{19}Ne beam of 10.1 MeV

Ref. M. Couder, PhD Thesis July 2004, Louvain-La-Neuve

ARES

Recoil Separator
with a
Wien Filter



Recoil Separator St. George

Study of (α, γ) [and (p, γ)] of astrophysics importance,
for $A < \approx 40$ targets,
emphasis on low energies, i.e. very small cross sections,
max. energy of 4 MeV/A

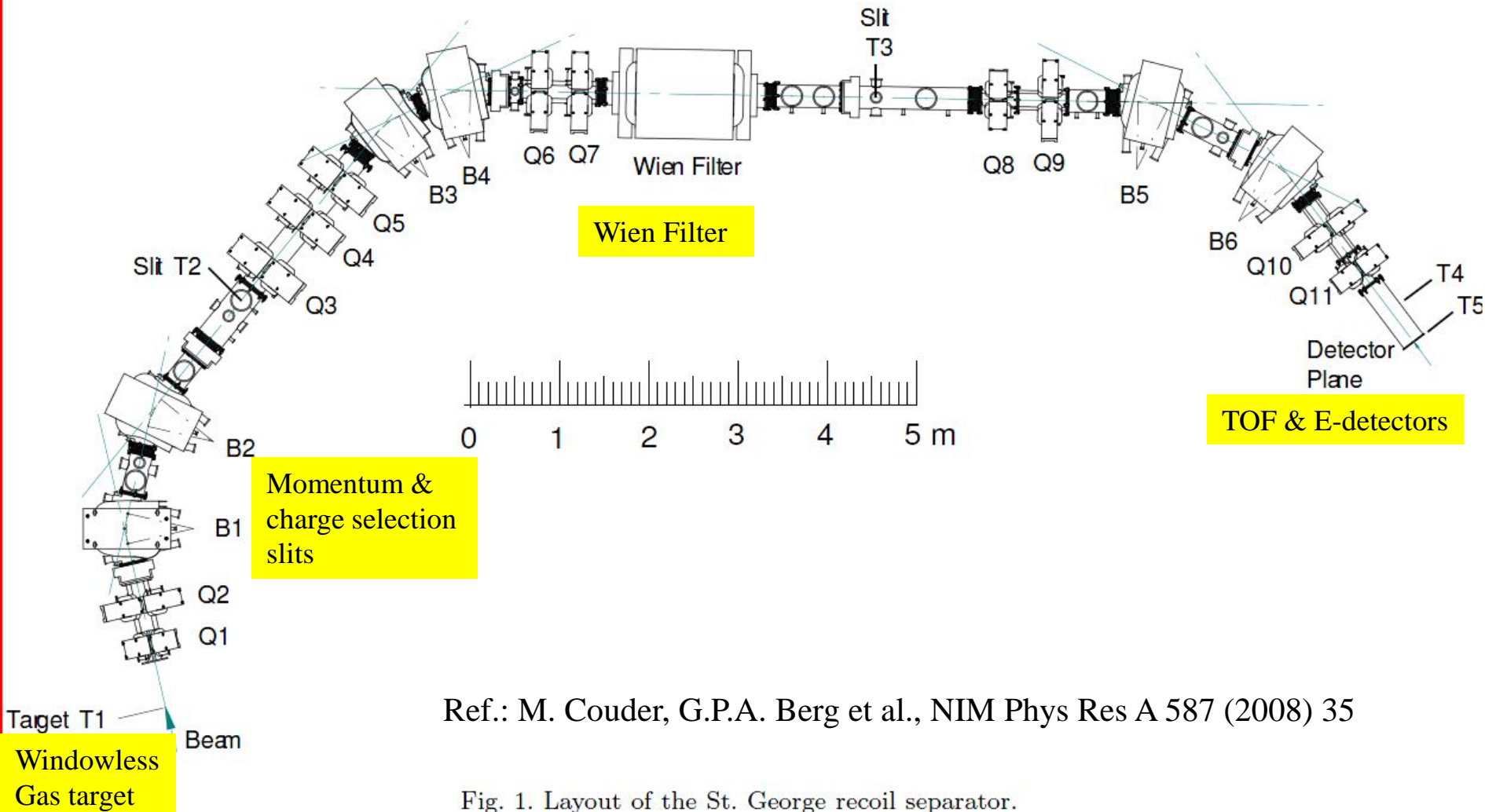
An overview of reaction result in the following
DESIGN PARAMETERS

Maximum magnetic rigidity $B\rho$: 0.45 Tm
Minimum magnetic rigidity $B\rho$: 0.10 Tm
Momentum acceptance dp : +/- 3.7 %
Angle acceptance, horiz & vert.: +/- 40 mrad

Further design considerations:

- Two phase construction
- Charge selection by $B\rho$ analysis (typical: 50% Transmission)
- High mass resolution ($\Delta m/m \cong 100$, 1st phase with 2 Wien Filters)
- Higher mass resolution ($\Delta m/m \cong 600$) 2nd phase
- Wien Filters for mass resolution (energy too low for “Wedge” method)

St. George, Layout



Ref.: M. Couder, G.P.A. Berg et al., NIM Phys Res A 587 (2008) 35

Fig. 1. Layout of the St. George recoil separator.

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

Electric force
Magnetic force

(1)

The Wien Filter

$F = 0$ when $qE = qv \times B$ with $E \perp B$

$v = E/B$ with $E \perp B$ (22)

$v \neq E/B$

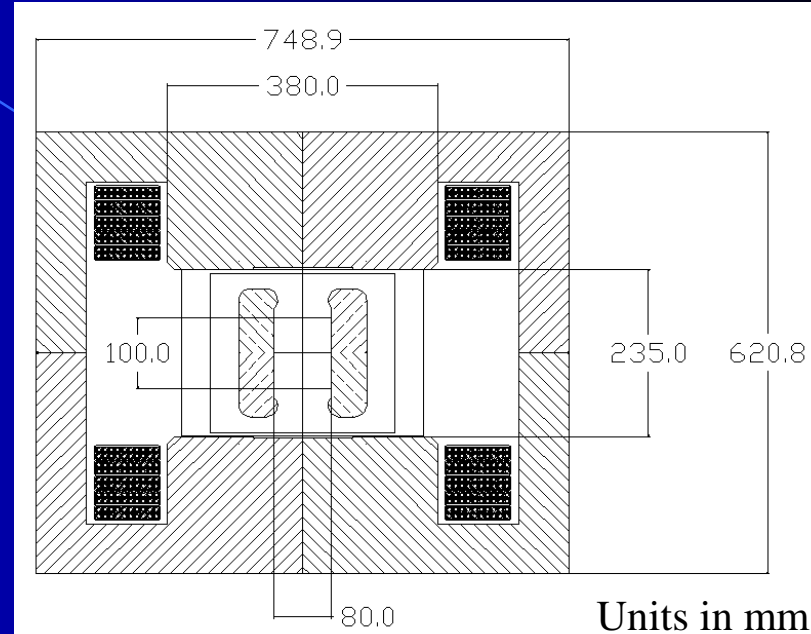
$F = (m/q)a = E + vB$

$a = \text{acceleration}$

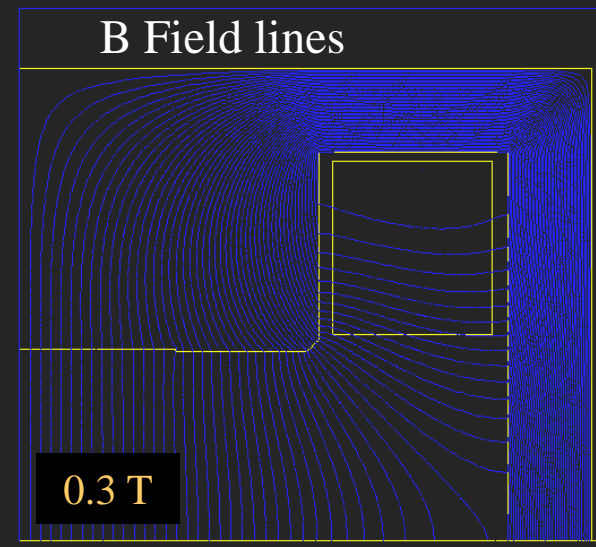
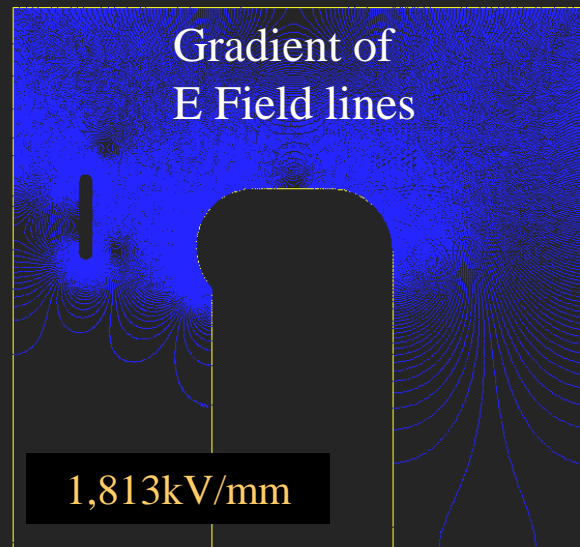
Leads to m/q separation

Select q before Wien Filter

Design study of
Wien Filter
for St. George

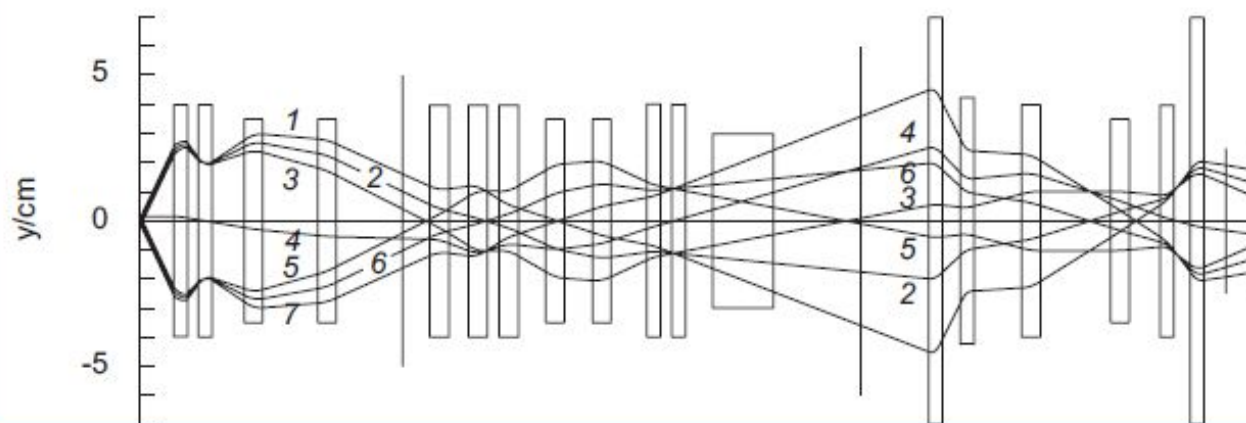
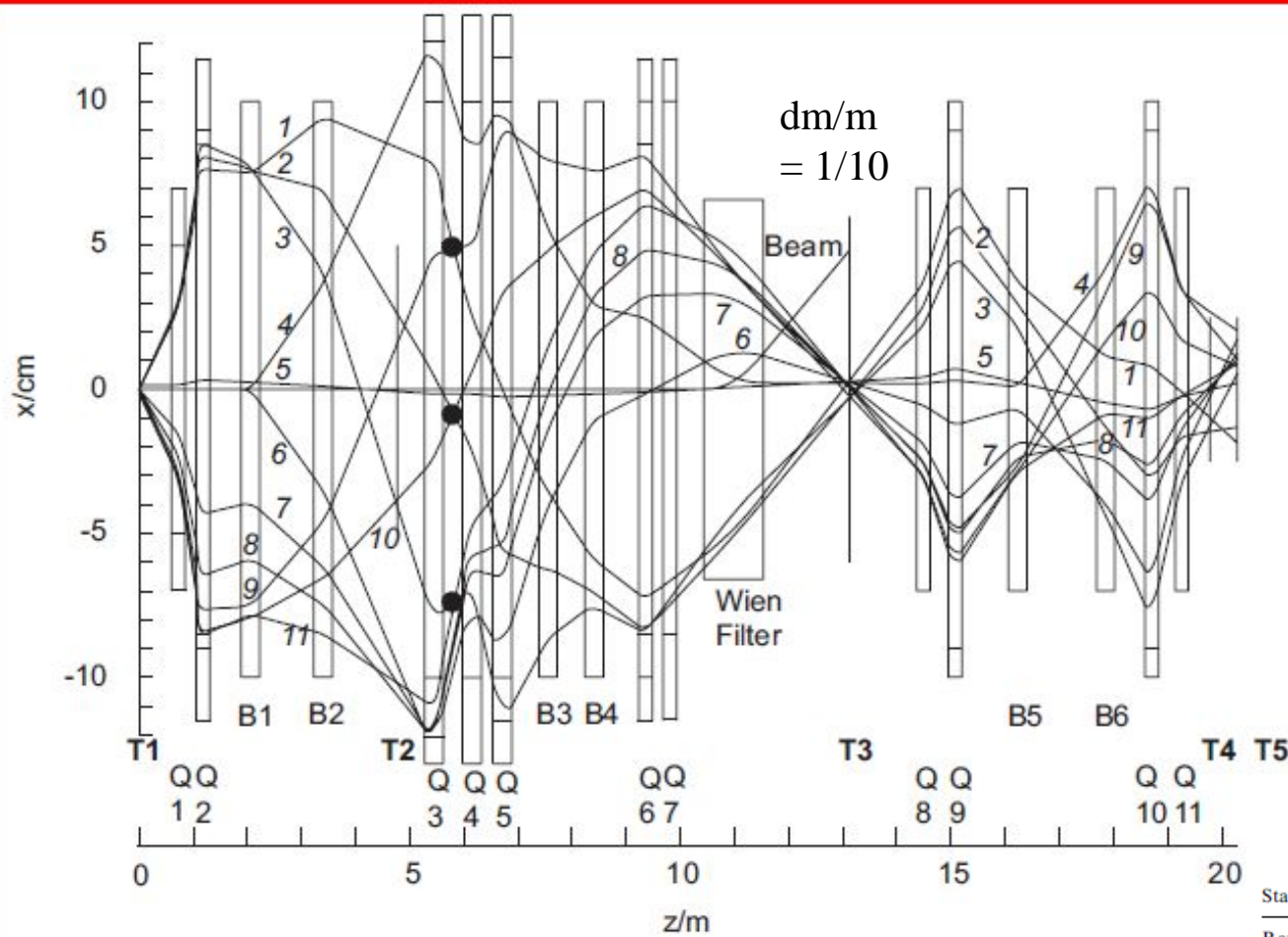


Electrostatic system of
Danfysik Wien Filter



St. George Ion-optics

Characteristic rays



Starting values of the 11 horizontal and 7 vertical rays shown in Fig. 2

Ray number	Horizontal rays			Vertical rays	
	x (mm)	θ (mrad)	$\delta E/E$ (%)	y (mm)	ϕ (mrad)
1	0	40	7.5	-1.5	40
2	0	40	0	0	40
3	0	40	-7.5	1.5	40
4	0	0	13	1.5	0
5	1.5	0	0	1.5	-40
6	0	0	-10.5	0	-40
7	0	-20	-9.5	-1.5	-40
8	0	-30	-9.0		
9	0	-40	7.5		
10	1.5	-40	0		
11	0	-40	-7.5		
Beam	0	0	0		

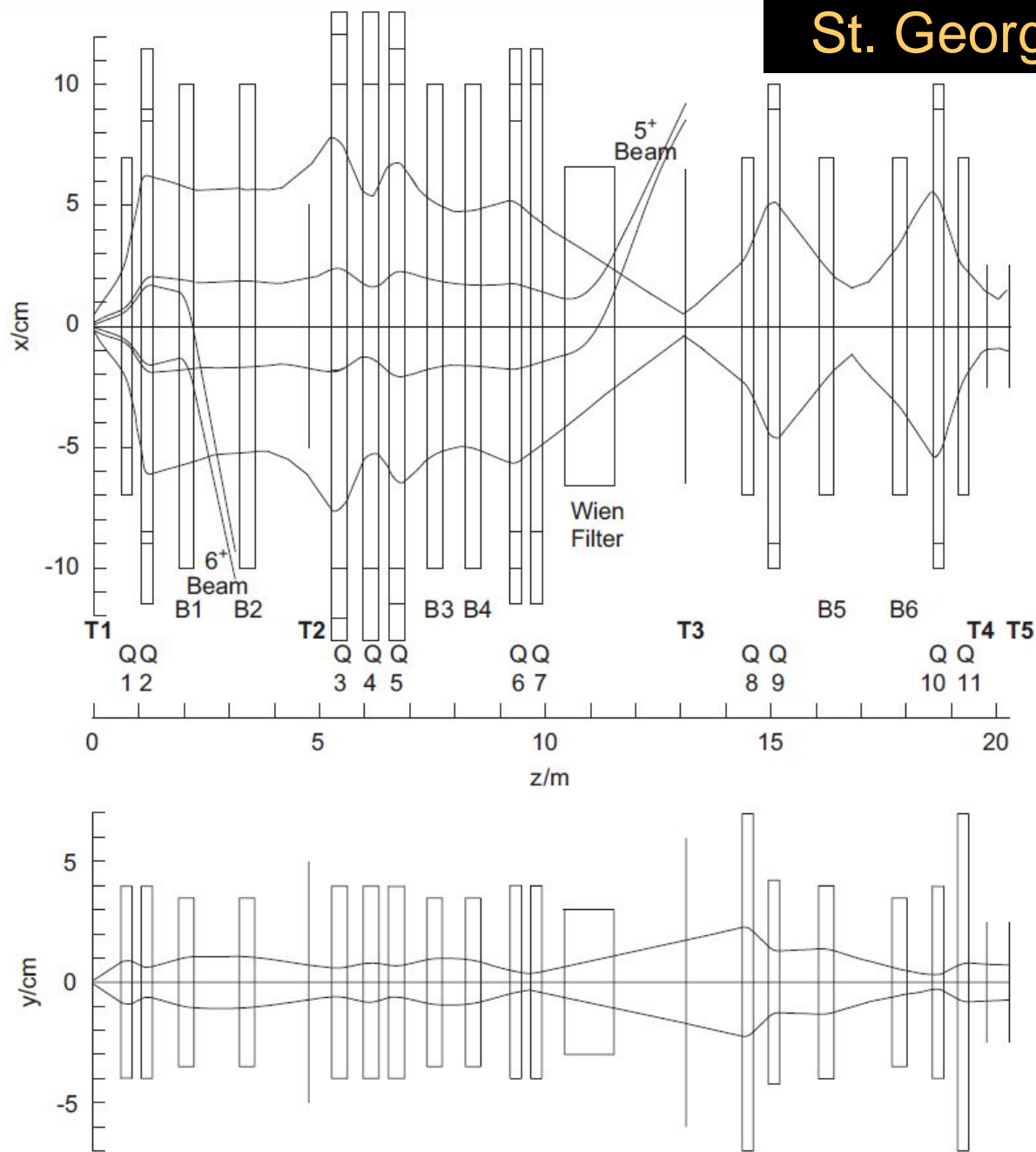


Fig. 3. Ion optics of the $^{22}\text{Ne}(\alpha, \gamma)^{26}\text{Mg}$ reaction in inverse kinematics at 4.6 MeV incident energy. Shown are the horizontal envelopes of the 5^+ reaction products, and the most abundant 5^+ and the 6^+ beams. The lower panel shows the vertical envelope of the reaction products.

St. George Wien Filter (velocity filter)

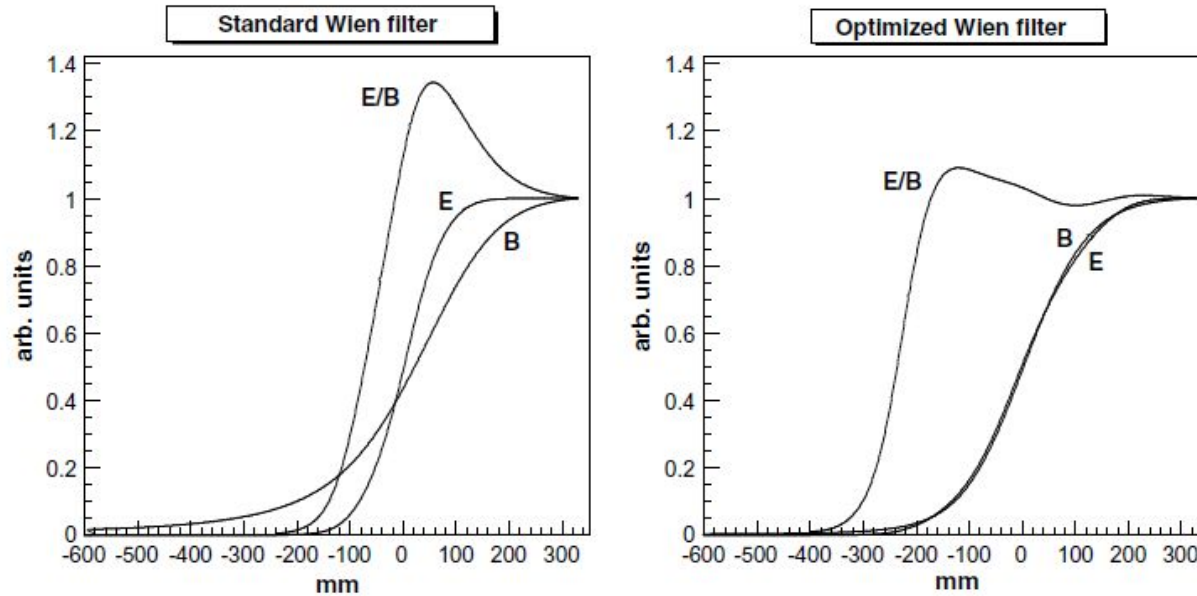


Fig. 3. Fringe field comparison of a standard Wien filter (left panel) and the newly designed (right panel). The ratio of the fields is also shown.

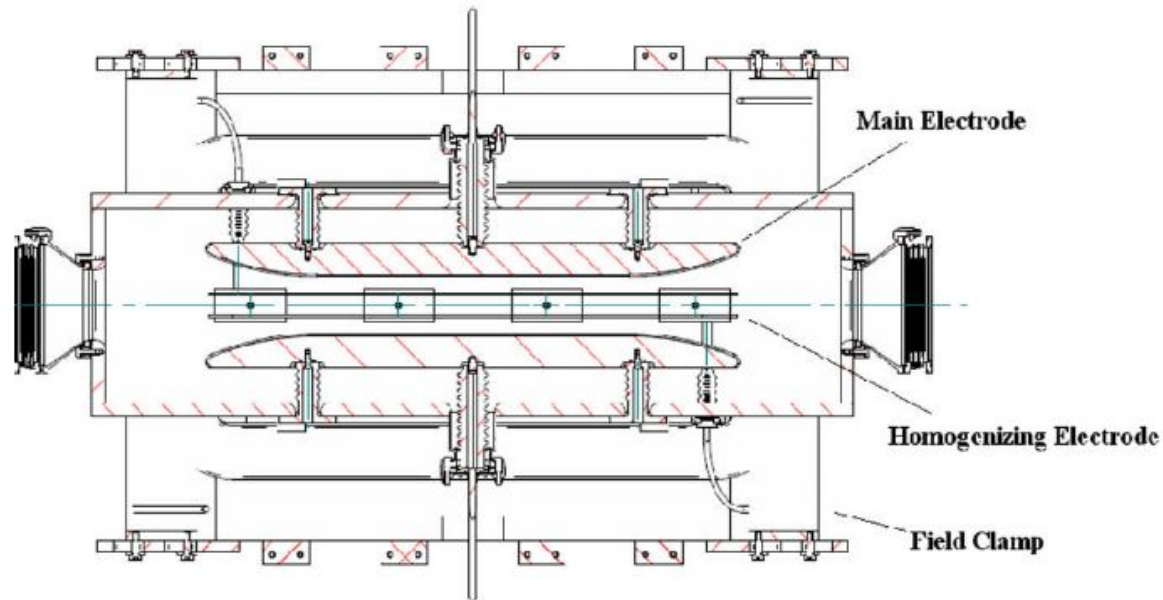


Fig. 4. A top view of the horizontal midplane of the Wien filter is shown. Electrostatic dipole is mounted inside the magnet.

SECAR

- SECAR radiative capture on unstable beams, can only be measured in inverse kinematics
- Designed to make use of high-intensity FRIB beams
- Up to masses $A = 65$ to cover the expected mass range of the rp process, (p, γ)
- Beam rejection 10^{17} , therefore mass separation $m/dm > 750$
- 4 ion-optical sections, charge selection, first Wien Filter, second Wien Filter, clean-up section
- Energy range $E_{\text{cm}} = 0.2 - 3 \text{ MeV}$

Broad Set of Reactions Define Rigidity and Acceptance Parameters

Charge B

Reaction	E_{cm} Beam MeV	Q- value MeV	dE/E Range %	Recoil Charge q	Half Angle, Recoil mrad	$B\rho$ Recoil Tm	$E\rho$ Recoil MV	$B\rho$ Beam Tm
$^{15}\text{O}(\alpha,\gamma)^{19}\text{Ne}$	0.5	3.529	± 3.1	3	± 15.6	0.29	1.25	0.14
	3	3.529	± 2.1	6	± 10.3	0.35	3.75	0.35
$^{44}\text{Ti}(\alpha,\gamma)^{48}\text{Cr}$	0.5	7.696	± 2.3	4	± 11.7	0.58	2.74	0.19
	3	7.696	± 1.3	10	± 6.2	0.57	6.59	0.48
$^{19}\text{Ne}(p,\gamma)^{20}\text{Na}$	0.2	2.193	± 1.3	4	± 6.4	0.31	1.88	0.21
	3	2.193	± 0.71	9	± 3.6	0.54	12.5	0.81
$^{23}\text{Mg}(p,\gamma)^{24}\text{Al}$	0.2	1.872	± 0.92	4	± 4.6	0.38	2.28	0.15
	3	1.872	± 0.56	11	± 2.8	0.53	12.4	0.58
$^{25}\text{Al}(p,\gamma)^{26}\text{Si}$	0.2	5.517	± 2.3	4	± 11.7	0.41	2.48	0.15
	3	5.517	± 0.90	11	± 4.5	0.58	13.5	0.58
$^{30}\text{P}(p,\gamma)^{31}\text{S}$	0.2	6.133	± 2.2	4	± 10.8	0.49	3.97	0.15
	3	6.133	± 0.80	12	± 4.0	0.63	14.8	0.58
$^{33}\text{Cl}(p,\gamma)^{34}\text{Ar}$	0.2	4.663	± 1.5	5	± 7.6	0.43	2.6	0.31
	3	4.663	± 0.6	14	± 3.1	0.59	14.0	1.19
$^{34}\text{Cl}(p,\gamma)^{35}\text{Ar}$	0.2	5.897	± 1.8	5	± 9.2	0.44	2.7	0.32
	3	5.897	± 0.7	14	± 3.5	0.61	14.4	1.22
$^{37}\text{K}(p,\gamma)^{38}\text{Ca}$	0.2	4.548	± 1.3	5	± 6.6	0.48	2.9	0.27
	3	4.548	± 0.54	15	± 2.7	0.62	14.6	1.04
$^{38}\text{K}(p,\gamma)^{39}\text{Ca}$	0.2	5.763	± 1.6	5	± 8.1	0.49	3.0	0.27
	3	5.763	± 0.61	15	± 3.1	0.64	15.0	1.06
$^{65}\text{As}(p,\gamma)^{66}\text{Se}$	0.2	2.030	± 0.35	6	± 1.8	0.70	4.3	0.18
	3	2.030	± 0.21	21	± 1.0	0.77	18.4	0.71

These reactions define the following required design parameters

- Even at highest energy most beams can be used for setup of experiments with sufficient count rate
- Otherwise less-abundant higher charge states can be used

Min. - Max. $B\rho$ 0.14- 0.80 Tm
Min. - Max $E\rho$ 1.0 - 19 MV

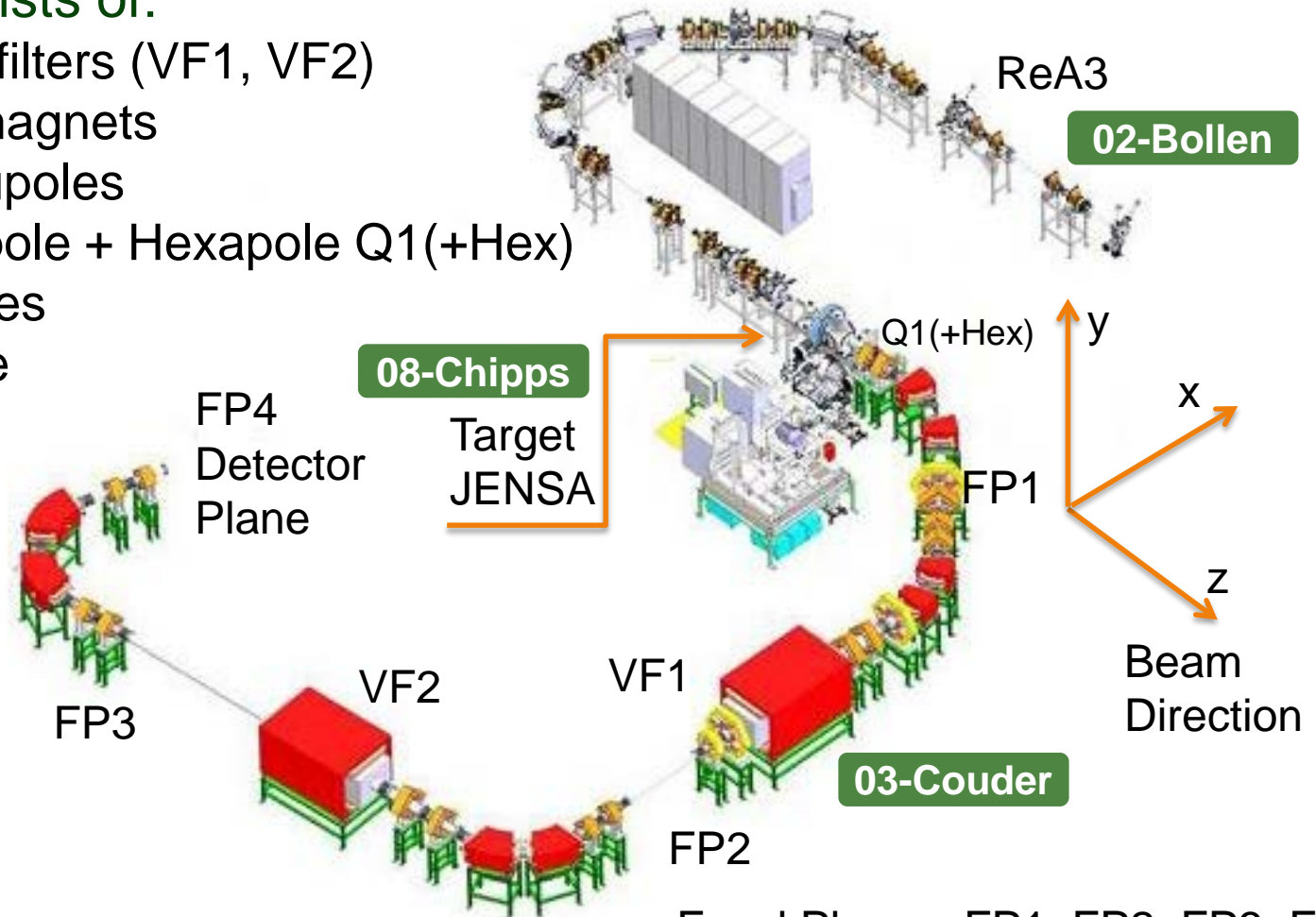
Angle Accept., x, y +/- 25 mrad
Energy Acceptance +/- 3.1 %

SECAR Layout

Charge B

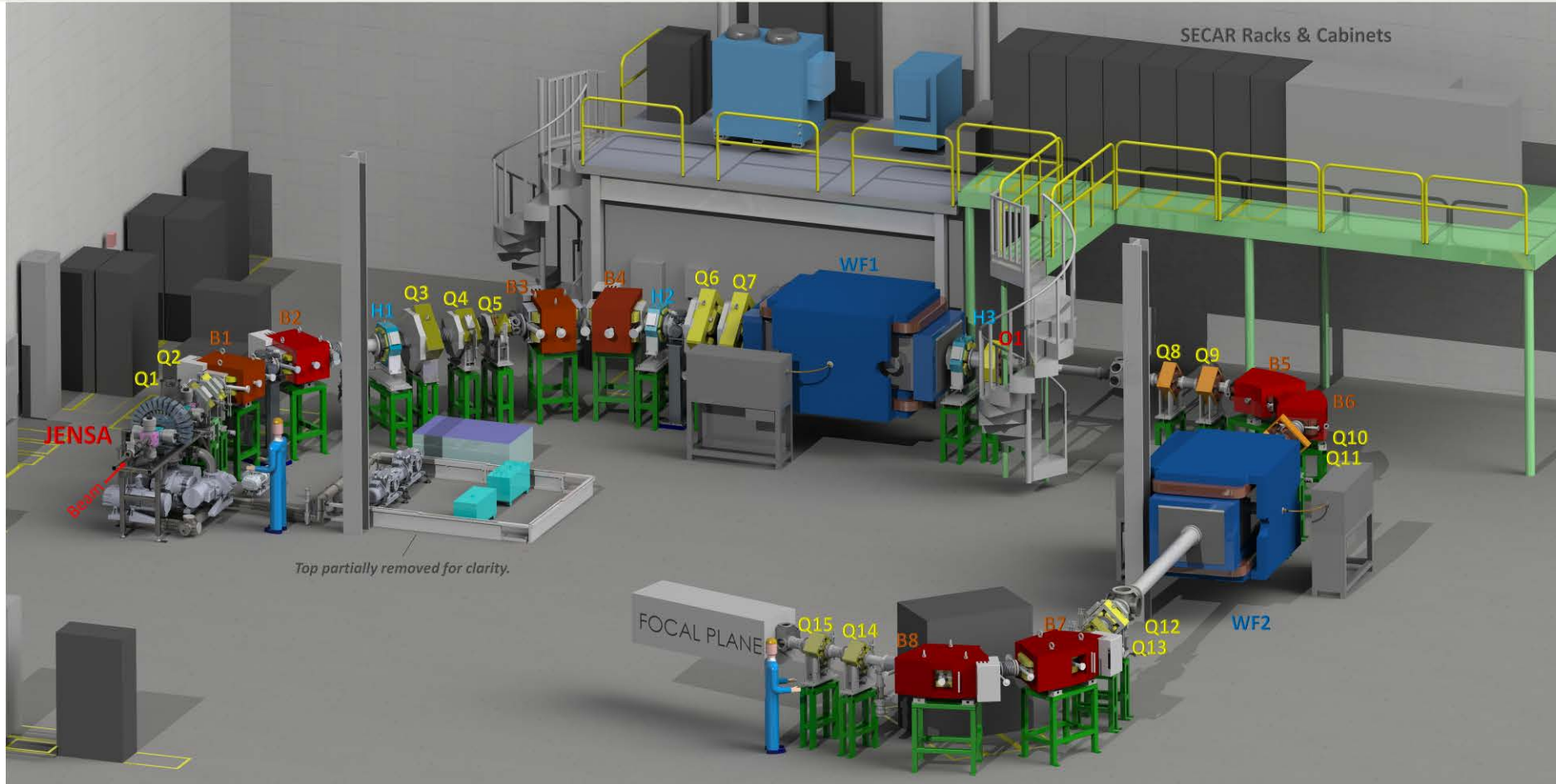
SECAR consists of:

- 2 Velocity filters (VF1, VF2)
- 8 Dipole magnets
- 14 Quadrupoles
- 1 Quadrupole + Hexapole Q1(+Hex)
- 3 Hexapoles
- 1 Octupole



Focal Planes: FP1, FP2, FP3, FP4

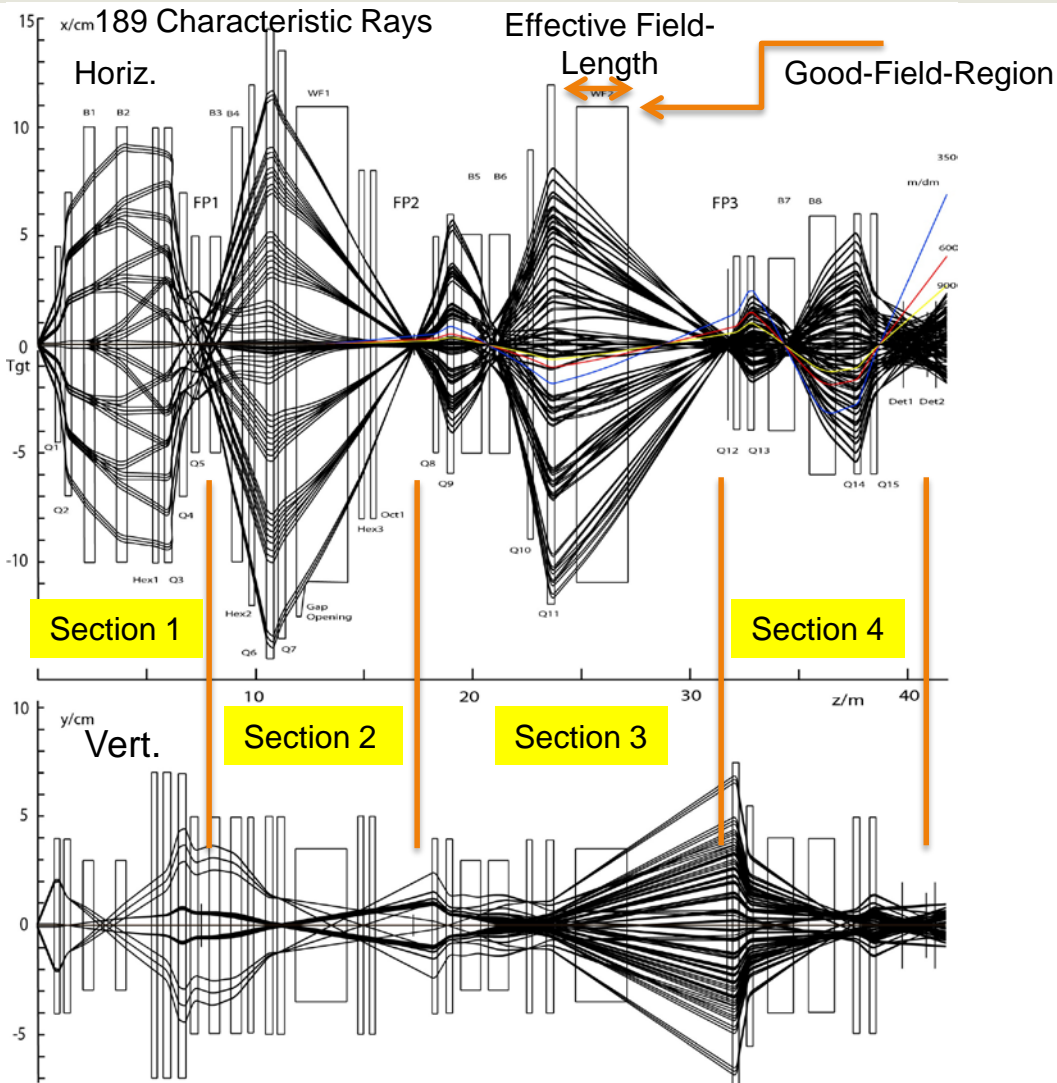
SECAR Recoil Separator for Astrophysical Capture Reactions



Separator for Capture Reactions

Ion Optics Optimized

Charge B



Section 1 Target to FP1
Charge state Selection
Dispersive focus

Section 2 FP1 to FP2
Mass Resolv. Power $R_m = 747$
Mass Resolution $R_{HO} = 508$
Achromatic focus

Section 3 FP2 to FP3
Mass Resolv. Power $R_m = 1283$
Mass Resolution = 767
Disp. $R_{16} = 0$, focus $R_{12} = 0$

Section 4 FP3 to Det1/Det2
Particle detection, HO correction
Cleanup section

Optimized up to 4th order, using
4 Hexapoles, 1 Octupole
Dipole edges up to 4th order

SECAR

End Lecture 3